Motivation Formalizing Sequential Constructiveness (SC) Wrap-Up

Motivation Formalizing Sequential Constructiveness (SC) C, Java vs. Synchronous Programming The Control Example A Constructive Game of Schedulability

Synchronous Languages—Lecture 13

Prof. Dr. Reinhard von Hanxleden

Christian-Albrechts Universität Kiel Department of Computer Science Real-Time Systems and Embedded Systems Group

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Sequentially Constructive Concurrency

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Slide 1

Formalizing Sequential Constructiveness (SC)

The 5-Minute Review Session

- 1. How do SCCharts and SyncCharts differ?
- 2. What does the initialize-update-read protocol refer to?
- 3. What is the SCG?
- 4. What are basic blocks? What are scheduling blocks?
- 5. When compiling from the SCG, what types of low-level synthesis do we distinguish? How do they compare?

Safety-Critical Embedded Systems



- Embedded systems often safety-critical
- Safety-critical systems must react deterministically
- ► Computations often exploit concurrency
- ► Key challenge: Concurrency must be deterministic!

Slide 3

Thanks to Michael Mendler (U Bamberg) for support with these slides

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Motivation

C, Java vs. Synchronous Programming

Formalizing Sequential Constructiveness (SC)

Implementing (Deterministic) Concurrency

C, Java, etc.:

- © Familiar
- © Expressive sequential paradigm
- © Concurrent threads unpredictable in functionality and timing

▶ Synchronous Programming:

- © predictable by construction
 - ⇒ Constructiveness
- © Unfamiliar to most programmers
- © Restrictive in practice

Aim: Deterministic concurrency with synchronous foundations, but without synchronous restrictions.

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Motivation

C, Java vs. Synchronous Programming

Formalizing Sequential Constructiveness (SC)

A Constructive Game of Schedulability

Motivation C, Java vs. Synchronous Programming Formalizing Sequential Constructiveness (SC) A Constructive Game of Schedulability

Comparing Both Worlds

Sequential Languages

- ► C. Java, ...
- ► Asynchronous schedule
 - o By default: Multiple concurrent readers/writers
 - o On demand: Single assignment synchronization (locks, semaphores)
- Imperative
 - o All sequential control flow prescriptive
 - o Resolved by programmer

Synchronous Languages

- Esterel, Lustre, Signal, SCADE, SyncCharts ...
- ► Clocked, cyclic schedule
 - o By default: Single writer per cycle, all reads initialized
 - o On demand: Separate multiple assignments by clock barrier (pause, wait)
- Declarative
 - All micro-steps sequential control flow descriptive
 - o Resolved by scheduler

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Motivation

C, Java vs. Synchronous Programming

Formalizing Sequential Constructiveness (SC)

Comparing Both Worlds (Cont'd)

Sequential Languages

- Asynchronous schedule
 - © No guarantees of determinism or deadlock freedom
 - © Intuitive programming paradigm

Synchronous Languages

- Clocked, cyclic schedule
 - Deterministic concurrency and deadlock freedom
 - Heavy restrictions by constructiveness analysis



Sequentially Constructive Model of Computation (SC MoC)

- © Deterministic concurrency and deadlock freedom
- Intuitive programming paradigm

Implementing Deterministic Concurrency: SC MoC

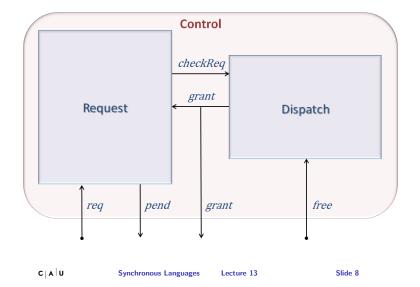
- Concurrent micro-step control flow:
 - ② Descriptive
 - Resolved by scheduler
 - ⇒ Deterministic concurrency and deadlock freedom
- **Sequential** micro-step control flow:
 - Prescriptive
 - Resolved by the programmer
 - ⇒ Intuitive programming paradigm

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Motivation Formalizing Sequential Constructiveness (SC)

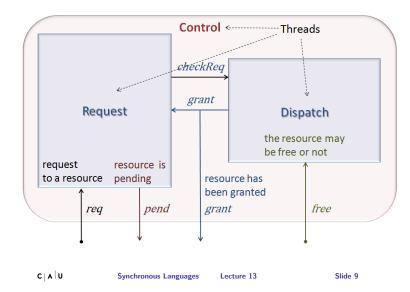
The Control Example

A Sequentially Constructive Program



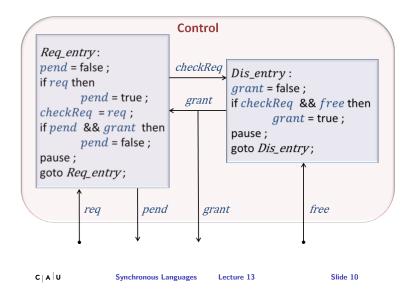
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A Sequentially Constructive Program (Cont'd)

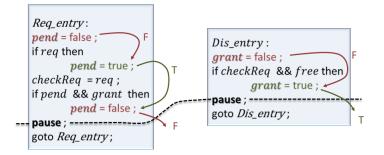


Motivation Formalizing Sequential Constructiveness (SC) The Control Example

A Sequentially Constructive Program (Cont'd)



A Sequentially Constructive Program (Cont'd)



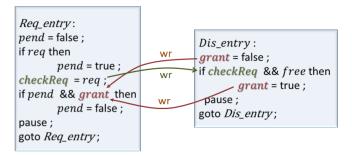
Imperative program order (sequential access to shared variables)

- "write-after-write" can change value sequentially
- Prescribed by programmer
 - Accepted in SC MoC
 - Not permitted in standard synchronous MoC

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Motivation Formalizing Sequential Constructiveness (SC) The Control Example

A Sequentially Constructive Program (Cont'd)



Concurrency scheduling constraints (access to shared variables):

- "write-before-read" for concurrent write/reads
- "write-before-write" (i. e., conflicts!) for concurrent & non-confluent writes
- Micro-tick thread scheduling prohibits race conditions
- Implemented by the SC compiler

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A Constructive Game of Schedulability logically reactive program





Programmer

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Sequential Admissibility - Basic Idea

- ► Sequentially ordered variable accesses
 - ► Are enforced by the programmer
 - ► Cannot be reordered by compiler or run-time platform
 - Exhibit no races
- Only concurrent writes/reads to the same variable
 - ► Generate potential data races
 - Must be resolved by the compiler
 - ► Can be ordered under multi-threading and run-time

The following applies to concurrent variable accesses only ...

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A Constructive Game of Schedulability

Organizing Concurrent Variable Accesses

SC Concurrent Memory Access Protocol (per macro tick)



concurrent, multi-writer, multi-reader variables



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Motivation Formalizing Sequential Constructiveness (SC)

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A Constructive Game of Schedulability

Goals and Challenges

The idea behind SC is simple – but getting it "right" not so!

What we are up to:

- 1. Want to be conservative wrt "Berry constructiveness"
 - ► An Esterel program should also be SC
- 2. Want maximal freedom without compromising determinacy
 - ► A determinate program should also be SC
 - ► An SC program must be determinate
- 3. Want to exploit sequentiality as much as possible
 - But what exactly is sequentiality?
- 4. Want to define not only the exact concept of SC, but also a practical strategy to implement it
 - ▶ In practice, this requires conservative approximations
 - ► Compiler must not accept Non-SC programs
 - Compiler may reject SC programs

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References

Most of the material here draws from this reference [TECS]:



R. von Hanxleden, M. Mendler, J. Aguado, B. Duderstadt, I. Fuhrmann, C. Motika, S. Mercer, O. O'Brien, and P. Roop.

Sequentially Constructive Concurrency – A Conservative Extension of the Synchronous Model of Computation.

ACM Transactions on Embedded Computing Systems, Special Issue on Applications of Concurrency to System Design, July 2014, 13(4s). https://rtsys.informatik.uni-kiel.de/~biblio/downloads/papers/tecs14.pdf

Unless otherwise noted, the numberings of definitions, sections etc. refer to this.

There is also an extended version [TR]:



R. von Hanxleden, M. Mendler, J. Aguado, B. Duderstadt, I. Fuhrmann, C. Motika, S. Mercer, O. O'Brien, and P. Roop.

Sequentially Constructive Concurrency – A Conservative Extension of the Synchronous Model of Computation.

Christian-Albrechts-Universität zu Kiel, Department of Computer Science, Technical Report 1308, ISSN 2192-6247, Aug. 2013, 13(4s). https://rtsys.informatik.uni-kiel.de/~biblio/downloads/papers/report-1308.pdf

Formalizing Sequential Constructiveness (SC)
Wrap-Up

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3] The SC Model of Computation [Sec. 4]

Overview

Motivation

Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3] The SC Model of Computation [Sec. 4]

Wrap-Up

Formalizing Sequential Constructiveness (SC)
Wrap-Up

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3] The SC Model of Computation [Sec. 4]

The Sequentially Constructive Language (SCL) [Sec. 2.1]

- Foundation for the SC MoC
- Minimal Language
- ► Adopted from C/Java and Esterel

$$s ::= x = e \mid s; s \mid \text{if } (e) s \text{ else } s \mid l : s \mid \text{goto } l \mid \text{fork } s \text{ par } s \text{ join } \mid \text{pause}$$

- Statement
- x Variable
- e Expression
- / Program label

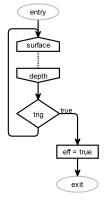
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Formalizing Sequential Constructiveness (SC)
Wrap-Up

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]

The SC Model of Computation [So

The SC Graph (SCG) [Sec. 2.3]



The concurrent and sequential control flow of an SCL program is given by an SC Graph (SCG)

Internal representation for

- Semantic foundation
- Analysis
- Code generation

SC Graph:

Labeled graph G = (N, E)

- Nodes N correspond to statements of sequential program
- Edges E reflect sequential execution control flow

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Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]

Formalizing Sequential Constructiveness (SC)
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Node Types in the SCG

Node $n \in N$ has statement type n.st

- ▶ $n.st \in$ {entry, exit, goto, x = ex, if (ex), fork, join, surf, depth}
- **x**: variable, **ex**: expression.

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Formalizing Sequential Constructiveness (SC)
Wrap-Up

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]

The SC Model of Computation [Sec. 4]

Edge Types in the SCG [Def. 2.1]

Define edge types:

- ightharpoonup iur-edges $\alpha_{iur} =_{def} \{ww, iu, ur, ir\}$
- ▶ instantaneous edges $\alpha_{ins} =_{def} \{seq\} \cup \alpha_{iur}$
- ▶ arbitrary edges $\alpha_a =_{\text{def}} \{ tick \} \cup \alpha_{ins}$
- ▶ flow edges $\alpha_{flow} =_{def} \{seq, tick\}$

Edge Types in the SCG [Def. 2.1]

Edge $e \in E$ has edge type $e.type \in \alpha_a$

- ► Specifies the nature of the particular ordering constraint expressed by *e*
- For $e.type = \alpha$, write $e.src \rightarrow_{\alpha} e.tgt$, pronounced "e.src α -precedes e.tgt"
- $ightharpoonup n_1
 ightharpoonup n_2$: sequential successors
- $ightharpoonup n_1
 ightharpoonup n_{tick} n_2$: tick successors
- ▶ $n_1 \rightarrow_{seq} n_2$, $n_1 \rightarrow_{tick} n_2$: flow successors, induced directly from source program
- ightharpoonup ightharpoonup reflexive and transitive closure of ightharpoonup
- Note: $n_1 \rightarrow_{seq} n_2$ does not imply fixed run-time ordering between n_1 and n_2 (consider loops)

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Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]

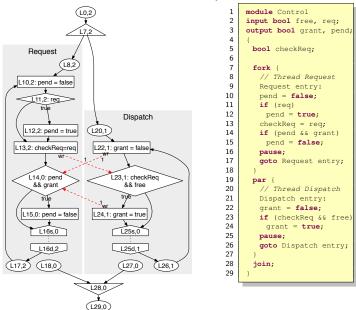
Mapping SCL & SCG

	Thread (Region)	Concurrency (Superstate)	Conditional (Trigger)	Assignment (Effect)	Delay (State)
SCG	entry	fork	c	x = e	surface
SCL	t	fork t ₁ par t ₂ join	if (c) s_1 else s_2	x = e	pause

Plus ";" (Sequence) and "goto" to specify sequential successors (solid edges)

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SCL & SCG – The Control Example



Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]

Sequentiality vs. Concurrency Static vs. Dynamic Threads

Recall: We want to distinguish between sequential and concurrent control flow.

But what do "sequential" / "concurrent" mean?

This distinction is not as easy to formalize as it may seem ...

To get started, distinguish

- ► Static threads: Structure of a program (based on SCG)
- Dynamic thread instance: thread in execution

Formalizing Sequential Constructiveness (SC)

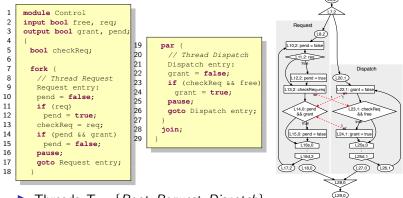
The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]

Static Threads [Sec. 2.4]

- ightharpoonup Given: SCG G = (N, E)
- Let T denote the set of threads of G
- T includes a top-level Root thread
- \blacktriangleright With each thread $t \in T$, associate unique
 - ightharpoonup entry node $t_{en} \in N$
 - ightharpoonup exit node $t_{ex} \in N$
- ▶ Each $n \in N$ belongs to a thread th(n) defined as
 - Immediately enclosing thread $t \in T$
 - \triangleright such that there is a flow path to n that originates in t_{en} , does not traverse t_{ex} , and does not traverse any other entry node t'_{en} , unless that flow path subsequently traverses t'_{ex} also
- \triangleright For each thread t, define sts(t) as the set of statement nodes $n \in N$ such that th(n) = t

```
<sup>1</sup>Added to definition in paper!
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Threads in Control Example



- ightharpoonup Threads $T = \{Root, Request, Dispatch\}$
- Root thread consists of the statement nodes $sts(Root) = \{L0, L7, L28, L29\}$
- ▶ The remaining statement nodes of *N* are partitioned into sts(Dispatch) and sts(Request)

Static Thread Concurrency and Subordination [Def. 2.2]

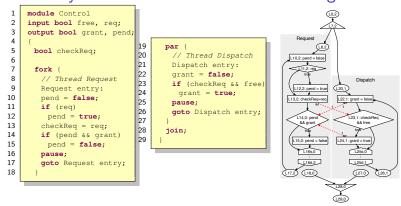
Let t, t_1 , t_2 be threads in T

- ightharpoonup fork(t) =_{def} fork node immediately preceding t_{en}
- For every thread $t \neq \text{Root}$: $p(t) =_{def} th(fork(t))$, the parent thread
- ▶ $p^*(t) =_{def} \{t, p(t), p(p(t)), \dots, \text{Root}\}$, the recursively defined set of ancestor threads of t
- \blacktriangleright t_1 is subordinate to t_2 , written $t_1 \prec t_2$, if $t_1 \neq t_2 \land t_1 \in p^*(t_2)$
- ▶ t_1 and t_2 are (statically) concurrent, denoted $t_1 || t_2$, iff t_1 and t_2 are descendants of distinct threads sharing a common fork node. *i. e.*:

 $\exists t_1' \in p^*(t_1), t_2' \in p^*(t_2) : t_1' \neq t_2' \land fork(t_1') = fork(t_2')$

- ▶ Denote this common fork node as $lcafork(t_1, t_2)$, the least common ancestor fork
- Lift (static) concurrency notion to nodes: $n_1 || n_2 \Leftrightarrow th(n_1) || th(n_2) \Leftrightarrow lcafork(n_1, n_2) = lcafork(th(n_1), th(n_2))$

Concurrency and Subordination in Control-Program



- ► Root ≺ Request and Root ≺ Dispatch
- ▶ Request || Dispatch, Root is not concurrent with any thread

Note: Concurrency on threads, in contrast to concurrency on node instances, is purely static and can be checked with a simple, syntactic analysis of the program structure.

Motivation
Formalizing Sequential Constructiveness (SC)

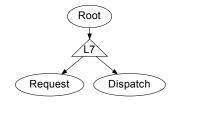
The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]

Thread Trees [TR, Sec. 3.7]

A Thread Tree illustrates the static thread relationships.

- Contains subset of SCG nodes:
 - 1. Entry nodes, labeled with names of their threads
 - 2. Fork nodes, attached to the entry nodes of their threads
- ► Similar to the AND/OR tree of Statecharts

Thread tree for Control example:



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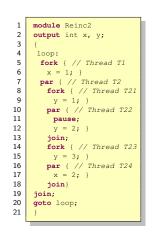
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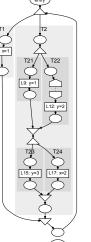
Formalizing Sequential Constructiveness (SC)
Wrap-Up

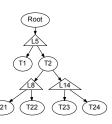
The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]

The SC Model of Computation [Sec. 4

Thread Trees - The Reinc2 Example







Alternative definition for static thread concurrency:

► Threads are concurrent iff their least common ancestor (Ica) in thread tree is a fork node

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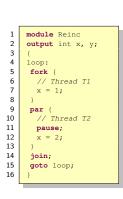
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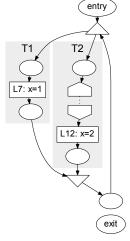
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Formalizing Sequential Constructiveness (SC)

Thread Reincarnation – The Reinc Example





Are interested in run-time concurrency, i. e., whether ordering is up to discretion of a scheduler.

Observations:

- ► T2 exhibits thread reincarnation
- Assignments to x are both executed in the same tick, yet are sequentialized
- ► Thus, static thread concurrency not sufficient to capture run-time concurrency!

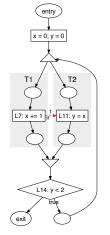
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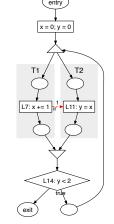
Statement Reincarnation I

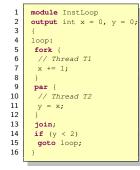


- module InstLoop output int x = 0, y 3 loop: fork { // Thread T1 x += 1;9 par { 10 // Thread T2 11 y = x;12 13 join; 14 **if** (y < 2) 15 goto loop; 16
- \triangleright Accesses to x in L7 and L11 executed twice within tick
- Denote this as statement reincarnation
- Accesses are (statically) concurrent
- ▶ Data dependencies ⇒ Must schedule L7 before *L*11
 - ▶ But only within the same loop iteration!

Not enough to impose an order on the program statements ⇒ Need to distinguish statement instances

Statement Reincarnation II





- © Traditional synchronous languages: Reject
- Instantaneous loops traditionally forbidden
- \odot SC: Determinate \Rightarrow Accept
- One might still want to ensure that a program always terminates
- But this issue is orthogonal to determinacy and having a well-defined semantics.

Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]
The SC Model of Computation [S

Macroticks [Def. 2.3 + 2.4]

- ightharpoonup Given: SCG G = (N, E)
- ▶ (Macro) tick R, of length $len(R) \in \mathbb{N}_{>1}$: mapping from micro tick indices $1 \le j \le len(R)$, to nodes $R(i) \in N$

A macro tick is also: Linearly ordered set of node instances

- Node instance: ni = (n, i), with statement node $n \in N$, micro tick count $i \in \mathbb{N}$
- ► Can identify macro tick R with set $\{(n, i) \mid 1 \le i \le len(R), n = R(i)\}$

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Motivation
Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]
Free Scheduling of SCGs [Sec. 3]

Run-Time Concurrency [Def. 2.5 + 2.6]

Given: macro tick R, index $1 \le i \le len(R)$, node $n \in N$ Def.: $last(n, i) = max\{j \mid j \le i, R(j) = n\}$, retrieves last occurrence of n in R at or before index i. If it does not exist, $last_R(n, i) = 0$.

Given: macro tick R, $i_1, i_2 \in \mathbb{N}_{\leq len(R)}$, and $n_1, n_2 \in N$. Def.: Two node instances $ni_1 = (n_1, i_1)$ and $ni_2 = (n_2, i_2)$ are (run-time) concurrent in R, denoted $ni_1 \mid_R ni_2$, iff

- 1. they appear in the micro ticks of R, i.e., $n_1 = R(i_1)$ and $n_2 = R(i_2)$,
- 2. they belong to statically concurrent threads, *i. e.*, $th(n_1) \mid\mid th(n_2)$, and
- 3. their threads have been instantiated by the same instance of the associated least common ancestor fork, *i. e.*, $last(n, i_1) = last(n, i_2)$ where $n = lcafork(n_1, n_2)$

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Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]

Free Scheduling of SCGs [Sec. 3]

The SC Model of Computation [Sec. 4]

Overview

Motivation

Formalizing Sequential Constructiveness (SC)

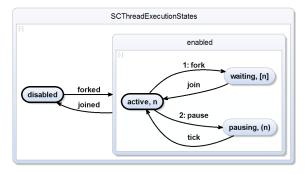
The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3] The SC Model of Computation [Sec. 4]

Wrap-Up

Continuations & Thread Execution States [Def. 3.1]

A continuation c consists of

- Node c.node ∈ N, denoting the current state of each thread, i. e., the node (statement) that should be executed next, similar to a program counter
- 2. Status $c.status \in \{active, waiting, pausing\}$



In a trace (see later slide), round/square/no parentheses around n = c.node denote c.status, for enabled continuations c

Formalizing Sequential Constructiveness (SC)
Wrap-Up

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2 Free Scheduling of SCGs [Sec. 3]
The SC Model of Computation [Sec. 4]

Continuation Pool & Configuration [Def. 3.2 + 3.3]

Continuation pool: finite set *C* of continuations

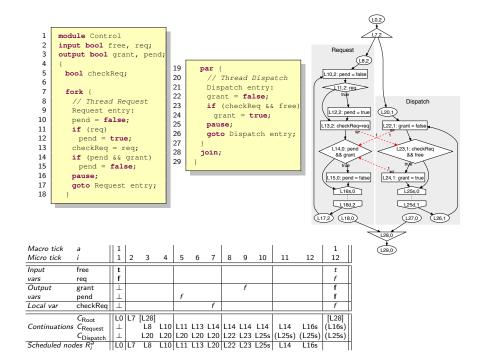
► C is valid if C meets some coherence properties (see [TECS]), e. g., threads in C adhere to thread tree structure

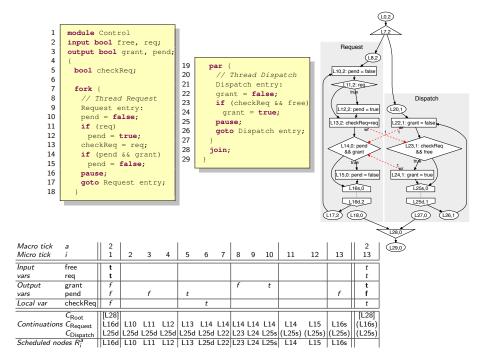
Configuration: pair (C, M)

- C is continuation pool
- ightharpoonup M is memory assigning values to variables accessed by G

A configuration is called valid if C is valid

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Motivation
Formalizing Sequential Constructiveness (SC)
Wrap-Up

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]

Free Scheduling of SCGs [Sec. 3]

The SC Model of Computation [Sec. 4]

Free Scheduling [Sec. 3.2]

Now define free scheduling, to set the stage for later defining "initialize-update-read" protocol $(\rightarrow SC\text{-admissible scheduling})$

Only restrictions:

- 1. Execute only ≺-maximal threads
 - ▶ If there is at least one continuation in C_{cur}, then there also is a ≺-maximal one, because of the finiteness of the continuation pool
- 2. Do so in an interleaving fashion

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Motivation T Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2 Free Scheduling of SCGs [Sec. 3]

Micro Steps I

Micro step: transition $(C_{cur}, M_{cur}) \xrightarrow{c}_{\mu s} (C_{nxt}, M_{nxt})$ between two micro ticks

- $ightharpoonup (C_{cur}, M_{cur})$: current configuration
- c: continuation selected for execution
- $ightharpoonup (C_{nxt}, M_{nxt})$: next configuration

The free schedule is permitted to pick any one of the \prec -maximal continuations $c \in C_{cur}$ with c.status = active and execute it in the current memory M_{cur}

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The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]

Free Scheduling of SCGs [Sec. 3]

The SC Model of Computation [Sec. 4]

Micro Steps II

Formalizing Sequential Constructiveness (SC)

(Recall:) Micro step: transition $(C_{cur}, M_{cur}) \xrightarrow{c}_{\mu s} (C_{nxt}, M_{nxt})$

- Executing c yields a new memory $M_{nxt} = \mu M(c, M_{cur})$ and a (possibly empty) set of new continuations $\mu C(c, M_{cur})$ by which c is replaced, i. e., $C_{nxt} = C_{cur} \setminus \{c\} \cup \mu C(c, M_{cur})$
- ▶ If $\mu C(c, M_{cur}) = \emptyset$: status flags set to active for all $c' \in C_{nxt}$ that become \prec -maximal by eliminating c from C
- Actions μM and μC (made precise in paper) depend on the statement *c.node.st* to be executed
- (C_{nxt}, M_{nxt}) uniquely determined by c, thus may write $(C_{nxt}, M_{nxt}) = c(C_{cur}, M_{cur})$

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Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]

Free Scheduling of SCGs [Sec. 3]

The SC Model of Computation [Sec. 4]

Clock Steps I

Quiescent configuration (C, M):

- ▶ No active $c \in C$
- ightharpoonup All $c \in C$ pausing or waiting

If $C = \emptyset$:

► Main program terminated

Otherwise:

► Scheduler can perform a global clock step

Formalizing Sequential Constructiveness (SC)
Wrap-Up

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]
Free Scheduling of SCGs [Sec. 3]
The SC Model of Computation [Sec. 4]

Clock Steps II

Global clock step: $(C_{cur}, M_{cur}) \rightarrow_{tick} (C_{nxt}, M_{nxt})$

- ► Transition between last micro tick of the current macro tick to first micro tick of the subsequent macro tick
- ▶ All pausing continuations of *C* advance from their surf node to the associated depth node:

$$C_{nxt} = \{c[\text{active} :: tick(n)] \mid c[\text{pausing} :: n] \in C_{cur}\} \cup \{c[\text{waiting} :: n] \mid c[\text{waiting} :: n] \in C_{cur}\}$$

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Motivation
Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]

Free Scheduling of SCGs [Sec. 3]

The SC Model of Computation [Sec. 4]

Clock Steps III

Global clock step updates the memory:

- Let $I = \{x_1, x_2, \dots, x_n\}$ be the designated input variables of the SCG, including input/output variables
- Memory is updated by a new set of external input values $V_I = [x_1 = v_1, \dots, x_n = v_n]$ for the next macro tick
- ► All other memory locations persist unchanged into the next macro tick.

Formally,

$$M_{n\times t}(x) = \left\{ egin{array}{ll} v_i, & ext{if } x = x_i \in I, \\ M_{cur}(x), & ext{if } x
otin I. \end{array}
ight.$$

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Macro Ticks

Scheduler runs through sequence

$$(C_0^a, M_0^a) \stackrel{c_1^a}{\rightarrow}_{\mu s} (C_1^a, M_1^a) \stackrel{c_2^a}{\rightarrow}_{\mu s} \cdots \stackrel{c_{k(a)}^a}{\rightarrow}_{\mu s} (C_{k(a)}^a, M_{k(a)}^a)$$
(1)

to reach final quiescent configuration $(\mathit{C}^{\mathit{a}}_{\mathit{k}(\mathit{a})}, \mathit{M}^{\mathit{a}}_{\mathit{k}(\mathit{a})})$

Sequence (1) is macro tick (synchronous instant) a:

$$(R^a, V_I^a): (C_0^a, M_0^a) \Longrightarrow (C_{k(a)}^a, M_{k(a)}^a)$$
 (2)

- V_I^a : projects the initial input, $V_I^a(x) = M_0^a(x)$ for $x \in I$
- $ightharpoonup M_{k(a)}^a$: response of a

Ra: sequence of statement nodes executed during a

- ▶ $len(R^a) = k(a)$ is length of a
- ▶ R^a is function mapping each micro tick index $1 \le j \le k(a)$ to node $R^a(j) = c_i^a$.node executed at index j

Motivation Formalizing Sequential Constructiveness (SC) Wrap-Up

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]
The SC Model of Computation [Sec. 4]

Runs and Traces

Run of G: sequence of macro ticks R^a and external inputs V_I^a , with

- initial continuation pool $C_0^0 = \{c_0\}$ activates the entry node of the G's Root thread, i.e., $c_0.node = \text{Root.}en$ and $c_0.status = \text{active}$
- ▶ all macro tick configurations are connected by clock steps, i.e., $(C_{k(a)}^a, M_{k(a)}^a) \rightarrow_{tick} (C_0^{a+1}, M_0^{a+1})$

Trace: externally visible output values at each macro tick R [TR, Sec. 3.9]

Formalizing Sequential Constructiveness (SC)
Wrap-Up

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]
Free Scheduling of SCGs [Sec. 3]
The SC Model of Computation [Sec. 4]

Determinacy

Recall:

- ▶ Macro (tick) configuration: end points of a macro tick (2)
- Micro (tick) configuration: all other intermediate configurations (C_i^a, M_i^a) , 0 < i < k(a) seen in (1)

Synchrony hypothesis:

- only macro configurations are observable externally (in fact, only the memory component of those)
- ► Suffices to ensure that sequence of macro ticks ⇒ is determinate
- lacktriangle Micro tick behavior $ightarrow_{\mu s}$ may well be non-determinate

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Motivation
Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]

Active and Pausing Continuations are Concurrent [TR, Prop. 2]

Given:

- \triangleright (C, M), reachable (micro or macro tick) configuration
- ▶ $c_1, c_2 \in C$, active or pausing continuations with $c_1 \neq c_2$

Then:

- $ightharpoonup c_1.node
 eq c_2.node$
- ightharpoonup th(c₁.node) || th(c₂.node)
- No instantaneous sequential path from c₁.node to c₂.node or vice versa

(Proof: see [TR])

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Concurrency vs. Sequentiality Revisited

Recall: Want to exploit sequentiality as much as possible

▶ Thus, consider only run-time concurrent data dependencies

- ► Consider Reinc example
- ▶ Thus, can ignore some statically concurrent data dependencies

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Formalizing Sequential Constructiveness (SC)
Wrap-Up

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]
The SC Model of Computation [Sec. 4]

Concurrency vs. Sequentiality Revisited II

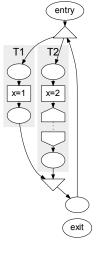
Question: Does (static) sequentiality preclude runtime concurrency?

- ► Then we could ignore data dependencies between nodes that are sequentially ordered
- ▶ But the answer is: **no**

Counterexample: Reinc3 (SCG shown on right)

- ► Assignments to x run-time concurrent? Yes!
- ► Assignments to x sequentially ordered? Yes!

Thus, concurrency and (static) sequentiality are not **mutually exclusive**, **but orthogonal!** However, (instantaneous) *run-time* sequentiality (on node *instances*) does exclude run-time concurrency



Notes on Free Scheduling I

Key to determinacy:

rule out uncertainties due to unknown scheduling mechanism

- Like the synchronous MoC, the SC MoC ensures macro-tick determinacy by inducing certain scheduling constraints on variable accesses
- Unlike the synchronous MoC, the SC MoC tries to take maximal advantage of the execution order already expressed by the programmer through sequential commands
- ► A scheduler can only affect the order of variable accesses through **concurrent** threads

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Motivation
Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2 Free Scheduling of SCGs [Sec. 3]
The SC Model of Computation [Sec. 4]

Notes on Free Scheduling II

Recall:

- ▶ If variable accesses (within tick) are already sequentialized by →_{seq}, they cannot appear simultaneously in the active continuation pool
- Hence, no way for thread scheduler to reorder them and thus lead to a non-determinate outcome

Similarly, threads are not concurrent with parent thread

- ▶ Because of path ordering ≺, a parent thread is always suspended when a child thread is in operation
- ► Thus, not up to scheduler to decide between parent and child thread
- No race conditions between variable accesses performed by parent and child threads; no source of non-determinacy

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The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]

Free Scheduling of SCGs [Sec. 3]

The SC Model of Computation [Sec. 4]

The Aim

Want to find a suitable restriction on the "free" scheduler which is

- 1. easy to compute
- 2. leaves sufficient room for concurrent implementations
- still (predictably) sequentializes any concurrent variable accesses that may conflict and produce unpredictable responses

In the following, will define such a restriction: the SC-admissible schedules

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Motivation Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]

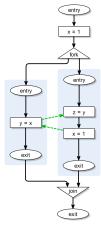
Guideline for SC-admissibility

- ▶ Initialize-Update-Read protocol, for concurrent accesses
- ► Want to conservatively extend Esterel's "Write-Read protocol" (must do emit *before* testing)
- ▶ But does Esterel *always* follow write-read protocol?

Write After Read Revisited

```
module WriteAfterRead
output x, y, z;
emit x;
[
 present x then
  emit y
  end
!!
 present y then
  emit z
  end;
  emit x
]
```

```
module WriteAfterRead
output int x, y, z;
{
  x = 1;
  fork
   y = x;
  par
   z = y;
   x = 1;
  join
}
```



SCL version

Esterel version

SCG

- ► Concurrent emit *after* present test
- ▶ But WriteAfterRead is BC hence should also be SC!
- ▶ Observation: second emit is ineffective, *i. e.*, does not change value

Ineffectiveness – 1st Try [TR, Sec. 5.2]

```
module InEffective1
   output int x = 2;
3
     int v;
4
 5
     fork
      if (x == 2) {
        y = 1;
        x = 7
9
10
       else
11
        y = 0
12
13
14
     join
15
```

If L13 is scheduled before L6:

- ► L13 is effective
- ► No out-of-order write
- ► y = 0

If L13 is scheduled after L8 (and L6):

- ► L13 is out-of-order write
- ► However, L13 is ineffective
- $ightharpoonup y = 1 (\rightarrow non-determinacy!)$
- ► The problem: L8 hides the potential effectiveness of L13 wrt. L6!
- ▶ Both schedules would be permitted under a scheduling regime that permits ineffective writes
- ightharpoonup Strengthen notion of "ineffective writes":
- ► Consider writes "ineffective" only if they do not change read!

Ineffectiveness – 2nd Try

```
1
    module InEffective2
2
    output bool x = false;
3
     int y;
4
5
    fork
     if (!x) {
7
       y = 1;
8
        x = x xor true
9
10
      else
11
       y = 0
12
13
     x = x xor true;
14
    join
15
```

```
x = x x or true
```

- Relative writes
- ► Equivalent to "x = !x"

Sequence L13; L6; L11:

ightharpoonup y = 0

Sequence L6; L7; L8; L13:

- ▶ Q: Is L13 ineffective *relative to L6*?
- A: Yes!
- ► L13 is out-of-order . . .
- but writes x = true, which is what L6 read!
- $ightharpoonup y = 1 (\rightarrow again non-determinacy!)$
- ► Again, both schedules would be permitted under a scheduling regime that permits ineffective writes
- ► → Replace "ineffectiveness" by "confluence"

Formalizing Sequential Constructiveness (SC)
Wrap-Up

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]
The SC Model of Computation [Sec. 4]

Overview

Motivation

Formalizing Sequential Constructiveness (SC)

```
The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3] The SC Model of Computation [Sec. 4]
```

Wrap-Up

Motivation
Formalizing Sequential Constructiveness (SC)
Wran-Un

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]

The SC Model of Computation [Sec. 4]

Combination Functions [Def. 4.1]

Combination function f:

- ► $f(f(x, e_1), e_2) = f(f(x, e_2), e_1)$ for all x and all side-effect free expressions e_1, e_2
- ▶ Sufficient condition: *f* is *commutative* and *associative*
- Examples: *, +, -, max, and, or

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Formalizing Sequential Constructiveness (SC)
Wran-Un

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]
The SC Model of Computation [Sec. 4]

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Relative and Absolute Writes [Def. 4.2]

Relative writes, of type f ("increment" / "modify"): x = f(x, e)

- f must be a combination function
- ▶ Evaluation of *e* must be free of side effects
- Thus, schedules ' $x = f(x, e_1)$; $x = f(x, e_2)$ ' and ' $x = f(x, e_2)$; $x = f(x, e_1)$ ' yield same result for x
- ► Thus, writes are confluent
- ► E.g., x++, x = 5*x, x = x-10

Absolute writes ("write" / "initialize"): x = e

- Writes that are not relative
- ► E.g., x = 0, x = 2*y+5, x = f(z)

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iur Relations [Def. 4.3]

Given two statically concurrent accesses $n_1 \parallel n_2$ on some variable x, we define the iur relations

- ▶ $n_1 \rightarrow_{ww} n_2$ iff n_1 and n_2 both initialize x or both perform updates of different type. We call this a www conflict
- $ightharpoonup n_1
 ightharpoonup n_2$ iff n_1 initializes x and n_2 updates x
- $ightharpoonup n_1
 ightharpoonup n_2$ iff n_1 updates x and n_2 reads x
- ▶ $n_1 \rightarrow_{ir} n_2$ iff n_1 initializes x and n_2 reads x

Since $n_1 \rightarrow_{ww} n_2$ implies $n_2 \rightarrow_{ww} n_1$:

- ▶ abbreviate the conjunction of $n_1 \rightarrow_{ww} n_2$ and $n_2 \rightarrow_{ww} n_1$ with $n_1 \leftrightarrow_{ww} n_2$
- ightharpoonup by symmetry $ightharpoonup_{ww}$ implies \leftrightarrow_{ww}

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Synchronous Languages

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Motivation
Formalizing Sequential Constructiveness (SC)
Wrap-Up

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]

The SC Model of Computation [Sec. 4]

Confluence of Nodes [Def. 4.4]

Given:

- ► Valid configuration (*C*, *M*) of SCG
- ▶ Nodes $n_1, n_2 \in N$

 n_1, n_2 are conflicting in (C, M) iff

- 1. n_1, n_2 active in C, i. e., $\exists c_1, c_2 \in C$ with $c_i.status = active$ and $n_i = c_i.node$
- 2. $c_1(c_2(C, M)) \neq c_2(c_1(C, M))$

 n_1 , n_2 are confluent with each other in (C, M), written: $n_1 \sim_{(C, M)} n_2$, iff

▶ \not Sequence of micro steps $(C, M) \rightarrow_{\mu s} (C', M')$ such that n_1 and n_2 are conflicting in (C', M')

Notes on Confluence

(From definition:) $n_1 \sim_{(C,M)} n_2$ iff

Formalizing Sequential Constructiveness (SC)

▶ \not Sequence of micro steps $(C, M) \rightarrow_{\mu s} (C', M')$ such that n_1 and n_2 are conflicting in (C', M')

Observations I

- ► Confluence is taken *relative* to valid configurations (*C*, *M*) and *indirectly* as the absence of conflicts
- ► Instead of requiring that confluent nodes commute with each other for arbitrary memories, we only consider those configurations (C', M') that are reachable from (C, M)
- ▶ E. g., if it happens for a given program that in all memories M' reachable from a configuration (C, M) two expressions ex_1 and ex_2 evaluate to the same value, then the assignments $x = ex_1$ and $x = ex_2$ are confluent in (C, M)

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Motivation Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2 Free Scheduling of SCGs [Sec. 3]

The SC Model of Computation [Sec. 4]

Notes on Confluence

(From definition:) $n_1 \sim_{(C,M)} n_2$ iff

▶ $\not\exists$ Sequence of micro steps $(C, M) \rightarrow_{\mu s} (C', M')$ such that n_1 and n_2 are conflicting in (C', M')

Observations II

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- Similarly, if the two assignments are never jointly active in any reachable continuation pool C', they are confluent in (C, M), too
- Thus, statements may be confluent for some program relative to some reachable configuration, but not for other configurations or in another program
- ► However, notice that relative writes of the same type are confluent in the absolute sense, *i. e.*, for all valid configurations (*C*, *M*) of all programs

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Notes on Confluence

(From definition:) $n_1 \sim_{(C,M)} n_2$ iff

 \triangleright \exists Sequence of micro steps $(C, M) \rightarrow_{us} (C', M')$ such that n_1 and n_2 are conflicting in (C', M')

Observations III

- ▶ Confluence $n_1 \sim_{(C,M)} n_2$ requires conflict-freeness for all configurations (C', M') reachable from (C, M) by arbitrary micro-sequences under free scheduling
- ▶ Will use this notion of confluence to define the restricted set of SC-admissible macro ticks
- ► Since compiler will ensure SC-admissibility of the execution schedule.

one might be tempted to define confluence relative to these SC-admissible schedules;

however, this would result in a logical cycle

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Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] The SC Model of Computation [Sec. 4]

Notes on Confluence

(From definition:) $n_1 \sim_{(C,M)} n_2$ iff

 \triangleright $\not\exists$ Sequence of micro steps $(C, M) \rightarrow_{us} (C', M')$ such that n_1 and n_2 are conflicting in (C', M')

Observations IV

- ▶ This relative view of confluence keeps the scheduling constraints on SC-admissible macro ticks sufficiently weak
- ▶ Note: two nodes confluent in some configuration are still confluent in every later configuration reached through an arbitrary sequence of micro steps
- ▶ However, more nodes may become confluent in later configurations, because some conflicting configurations are no longer reachable
- Exploit this in following definition of confluence of node instances by making confluence of node instances within a macro tick relative to the index position at which they occur

Confluence of Node Instances [Def. 4.5]

Given:

- ▶ Macro tick R
- \triangleright (C_i, M_i) for 0 < i < len(R), the configurations of R
- Node instances $ni_1 = (n_1, i_1)$ and $ni_2 = (n_2, i_2)$ in R, i.e., $1 \le i_1, i_2 \le len(R), n_1 = R(i_1), n_2 = R(i_2)$

Call node instances confluent in R, written $ni_1 \sim_R ni_2$, iff

- for $i = min(i_1, i_2) 1$
- \triangleright $n_1 \sim_{(C_i,M_i)} n_2$

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InEffective2 Revisited

```
module InEffective2
   output bool x = false;
3
     int y;
    fork
      if (!x) {
10
      else
11
12
13
      x = x xor true;
14
    join
15
```

Recall sequence L6; L7; L8; L13:

- ▶ Q: Is L13 ineffective *relative to L6*?
- A: Yes!
- ► L13 is out-of-order . . .
- but writes x = false, which is what L6 read!
- Q: Are L6 and L13 confluent?
- ► A: No!
- ► L6 and L13 conflict at point of execution of L6

→ Def. of SC-admissibility – specifically, the underlying scheduling relations – uses confluence condition

Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]

The SC Model of Computation [Sec. 4]

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]
Free Scheduling of SCGs [Sec. 3]
The SC Model of Computation [Sec. 4]

Scheduling Relations [Def 4.6]

Given:

- ► Macro tick R with
- Node instances $ni_{1,2} = (n_{1,2}, i_{1,2})$, *i. e.*, $1 \le i_{1,2} \le len(R)$ and $n_{1,2} = R(i_{1,2})$
- $ightharpoonup ni_{1,2}$ concurrent in R, i.e., $ni_1 \mid_R ni_2$
- $ightharpoonup ni_{1,2}$ not confluent in R, i. e., $ni_1 \not\sim_R ni_2$

Then:

- $ightharpoonup ni_1
 ightharpoonup \frac{R}{\alpha} ni_2$ iff $n_1
 ightharpoonup n_2$ for some $\alpha \in \alpha_{iur}$
- $ightharpoonup ni_1
 ightharpoonup ^R ni_2$ iff $i_1 < i_2$; i. e., ni_1 happens before ni_2 in R.

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Formalizing Sequential Constructiveness (SC)
Wrap-Up

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]

The SC Model of Computation [Sec. 4]

Sequential Admissibility [Def. 4.7]

A macro tick R is SC-admissible iff

- ▶ for all node instances $ni_{1,2} = (n_{1,2}, i_{1,2})$ in R, with $1 \le i_{1,2} \le len(R)$ and $n_{1,2} = R(i_{1,2})$,
- ▶ for all $\alpha \in \alpha_{iur}$

the scheduling condition SC_{α} holds:

if $ni_1 \rightarrow_{\alpha}^R ni_2$ then $ni_1 \rightarrow^R ni_2$.

A run for an SCG is SC-admissible if all macro ticks R in this run are SC-admissible.

SC-admissibility vs. Determinacy

Formalizing Sequential Constructiveness (SC)

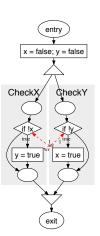
```
module NonDet
coutput bool x = false, y = false;

fork { // Thread CheckX}
if (!x)
    y = true;

par { // Thread CheckY}
if (!y)
    x = true
}

join
}
```

- ► Admissible runs? Yes, multiple
- ► Determinate? No



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Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]

The SC Model of Computation [Sec. 4]

SC-admissibility vs. Determinacy

```
module Fail
  output bool z = false;

fork {
    if (!z)
    z = true;
    }

    par {
        if (z)
        z = true
    }

    par {
        if (z)
        z = true
    }
}

par {
    if (z)
    z = true
    }
}
```

- Admissible runs? No
- ► Determinate? Yes

Thus: Determinacy ≠ SC-admissibility

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Sequential Constructiveness [Def. 4.8]



Definition: A program *P* is sequentially constructive (SC) iff for each initial configuration and input sequence:

- 1. There exists an SC-admissible run (P is reactive)
- 2. Every SC-admissible run generates the same determinate sequence of macro responses (*P* is determinate)

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Formalizing Sequential Constructiveness (SC)

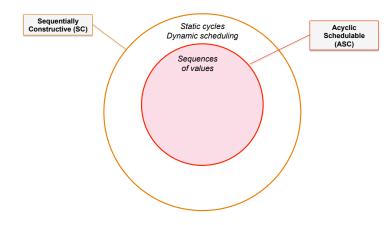
Synchronous Program Classes

Overview

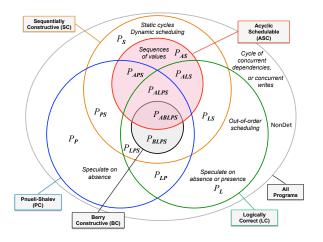
Wrap-Up

Synchronous Program Classes Summary

Synchronous Program Classes [TR, Sec. 9]

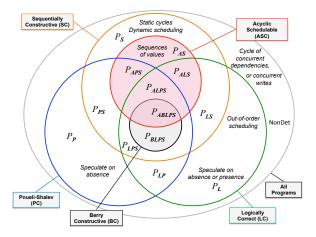


Synchronous Program Classes



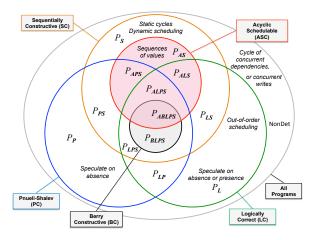
Example
$$P_{APS} = if(x) x = 1$$

Synchronous Program Classes



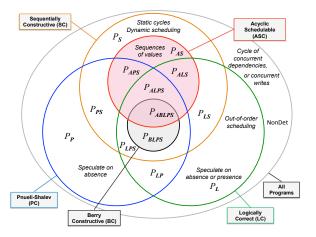
Example $P_{AS} = if (!x) x = 1$

Synchronous Program Classes



Example $P_{ALS} = if(!x) x = 1 else x = 1$

Synchronous Program Classes



Example
$$P_{ALPS} = \text{if (!x \&\& y) } \{x = 1; y = 1\}$$

Formalizing Sequential Constructiveness (SC)
Wrap-Up

Wrap-Up

Motivation
Synchronous Program Classes
Summary

Summary

Underlying idea of sequential constructiveness rather simple

- Prescriptive instead of descriptive sequentiality
- ► Thus circumventing "spurious" causality problems
- ► Initialize-update-read protocol

However, precise definition of SC MoC not trivial

- ► Challenging to ensure conservativeness relative to Berry-constructiveness
- ▶ Plain initialize-update-read protocol does not accommodate, e. g., signal re-emissions
- ► Restricting attention to *concurrent*, *non-confluent* node instances is key

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Motivation Formalizing Sequential Constructiveness (SC) Wrap-Up

Synchronous Program Classes
Summary

Motivation Formalizing Sequential Constructiveness (SC) Wrap-Up

Future Work

Synchronous Program Classes Summary

Conclusions

- ► Clocked, synchronous model of execution for imperative, shared-memory multi-threading
- ► Conservatively extends synchronous programming (Esterel) by standard sequential control flow (Java, C)
- ► ⇒ Deterministic concurrency with synchronous foundations, but without synchronous restrictions
 - Expressive and intuitive sequential paradigm
 - ▶ ② Predictable concurrent threads

Plenty of extensions/adaptations possible . . .

- ► Alternative notions of sequential constructiveness:
 - ► A truly "constructive" approach that sharpens SC admissibility to determinate schedules
 - Extension of iur-protocol, e.g., to model ForeC
- ▶ Improved synthesis & analysis see also next lecture

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