

Synchronous Languages—Lecture 06

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Esterel IV—The Constructive Semantics

The 5-Minute Review Session

1. What is the *state* of an Esterel program? Which implementation alternatives are there to memorize state?
2. What are implementation alternatives to interface with the environment, *e. g.*, a device that can be on or off?
3. What is the relationship between *events* and *states*?
4. What are possible examples for *causality problems*? What is the reason for these problems?
5. When is an Esterel program *logically reactive*? ... *correct*?

Overview

The Constructive Semantics

External Justification vs. Self-Justification
The Constructive Behavioral Semantics
The Constructive Operational Semantics

External Justification vs. Self-Justification

- ▶ Programming in Esterel:
 - ▶ Analyze input events to generate appropriate output signals
 - ▶ Use concurrent statements and intermediate local signals to create modular, well-structured programs
- ▶ Natural way of thinking:
 - ▶ Information propagation by *cause* and *effect*

```
present I then
  emit 0
end
```

External Justification vs. Self-Justification

```

module P1:
  input I;
  output O;
  signal S1, S2 in
    present I then emit S1 end
  ||
    present S1 else emit S2 end
  ||
    present S2 then emit O end
  end signal
end module

```

- ▶ Is this logically correct?
 - ▶ Yes!
- ▶ Is this well-behaved wrt information propagation?
 - ▶ Yes!

External Justification vs. Self-Justification

- ▶ “present S then p end”:
 - ▶ First test the status of S , then execute p if S is present
 - ▶ Status of S should not depend on what p might do
- ▶ Synchrony hypothesis:
 - ▶ Ordering implicit in the then word is not that of time, but that of sequential causality
- ▶ Want actual computation:
 - ▶ “Since S is present, we take the then branch”
- ▶ Don't want speculative computation:
 - ▶ “If we assume S present, then we take the then branch”

External Justification vs. Self-Justification

```

module P9:
  [
    present 01 then emit 01 end
  ]
  ||
  present 01 then
    present 02 else emit 02 end
  end
]

```

- ▶ Is this logically correct?
 - ▶ Yes!
- ▶ Is this well-behaved wrt information propagation?
 - ▶ No!
- ▶ Accepting P9 as correct is
 - ▶ Logically possible
 - ▶ But against (imperative) intention of the language

External Justification vs. Self-Justification

- ▶ Aside from the explicit concurrency “||”, all Esterel statements are sequential
- ▶ Want to preserve this in the semantics

```

module P10:
  present 0 then
    nothing;
  end;
  emit 0

```

- ▶ This is logically correct
- ▶ But still want to reject it:
 - ▶ In the logical semantics, the information that 0 is present flows backwards across the sequencing operator
 - ▶ Contradicts basic intuition about sequential execution

The Constructive Semantics

- ▶ Constructive semantics:
 - ▶ Does not check assumptions about signal statuses
 - ▶ Instead, propagates facts about control flow and signal statuses
- ▶ Three equivalent presentations:
 1. Constructive behavioral semantics
 2. Constructive operational semantics
 3. Circuit semantics

- ▶ The name *constructive semantics* is borrowed from constructive logic, in which one handles fact-propagating proofs, instead of handling values as in classical logic

The Constructive Semantics

1. Constructive behavioral semantics:
 - ▶ Derived from the logical behavioral semantics
 - ▶ Adds constructive restrictions to logical coherence rule
 - ▶ Is the simplest way of defining the language
2. Constructive operational semantics:
 - ▶ Based on an interpretation scheme expressed by term rewriting rules defining microstep sequences
 - ▶ Is the simplest way of defining an efficient interpreter
3. Circuit semantics:
 - ▶ Translation of programs into constructive circuits
 - ▶ Is the core of the Esterel v5 compiler

The Constructive Behavioral Semantics

- ▶ ... retains the spirit of the logical coherence semantics
- ▶ ... adds reasoning about what a program must or cannot do
- ▶ Define disjoint predicates to express
 - ▶ “A statement must terminate, must pause, must exit a trap T , or must emit a signal S ”
 - ▶ “A statement cannot terminate, cannot pause, cannot exit a trap T , or cannot emit a signal S ”
- ▶ The *Must* (*Cannot*) predicate determines
 - ▶ Which signals are present (absent)
 - ▶ Which statements are (cannot be) executed

The Constructive Behavioral Semantics

Recall: Logical Coherence Law

A signal S is present in an instant iff an “emit S ” statement is executed in this instant.

Replace with disjoint **Constructive Coherence Laws**:

*A signal S is present iff an “emit S ” statement must be executed.
A signal S is absent iff an “emit S ” statement cannot be executed*

The Constructive Behavioral Semantics

- ▶ Define *Must* and *Cannot* predicates by structural induction on statements
- ▶ A signal can have three statuses:
 - ▶ “+”: known to be **present**
 - ▶ “-”: known to be **absent**
 - ▶ “⊥”: yet **unknown**
- ▶ Is technically easier to define the *Cannot* predicate as the negation of a *Can* predicate
 - ▶ No constructiveness problem here as we only deal with finite sets

The Constructive Behavioral Semantics

$p; q$ (**Sequence**)

▶ Must (resp. can) execute q if p must (resp. can) terminate
present S then p else q end (**Test**)

- ▶ If S is known to be present:
 - ▶ Test behaves as p
- ▶ If S is known to be absent:
 - ▶ Test behaves as q
- ▶ If S is yet unknown:
 - ▶ Test can do whatever p or q can do
 - ▶ **There is nothing the test must do.** In particular, it does not even have to do what both p and q have to do—this is the essence of disallowing speculative execution.

The Constructive Behavioral Semantics

- ▶ Main novelty is in analysis of output and local signals
- ▶ Consider local signal here; output signal is similar

signal S in p end (**Local signal**)

Can predicate:

- ▶ Recursively analyze p with status \perp for S

The Constructive Behavioral Semantics

signal S in p end (Local signal)

Must predicate:

- ▶ Assume we already know that we must execute signal S in p end in some signal context E
- ▶ Must compute final status of S to determine signal context of p
- ▶ First analyze p in E augmented by setting the unknown status \perp for S
- ▶ If S must be emitted:
 - ▶ Propagate this information by **reanalyzing** p in E with S present
 - ▶ This may generate more information about the other signals
- ▶ Similarly, if we find that S cannot be emitted:
 - ▶ Reanalyze p in E with S absent

Accepting Programs

In the constructive behavioral semantics, a program is accepted as **constructive** iff fact propagation using the *Must* and *Can* (or *Cannot*) predicates suffices in establishing presence or absence of all output signals (and we can also compute a derivative—see later)

```

module P1:
  input I;
  output O;
  signal S1, S2 in
    present I then emit S1 end
  ||
    present S1 else emit S2 end
  ||
    present S2 then emit O end
  end signal
end module

```

- ▶ If I is present, then the first present statement must take its first branch, emit $S1$, and terminate. From this, we deduce that $S1$ is present. Then, the second present statement must take its (empty) then branch and cannot take its else branch. Since the “emit $S2$ ” statement cannot be executed, $S2$ cannot be emitted, which implies that $S2$ is absent. Finally, the third present statement cannot take its then branch, which implies that O cannot be emitted and is absent.
- ▶ If I is absent, then the first present statement cannot take its first branch, and the “emit $S1$ ” statement cannot be executed, which implies that $S1$ is absent. Therefore, the second present statement must take its then branch, the “emit $S2$ ” statement must be executed, which implies that $S2$ is present. Finally, the third present statement must take its then branch, and the “emit O ” statement must be executed, setting O present.

Accepting Programs

```

module P2:
  signal S in
    emit S;
    present 0 then
      present S then
        pause
      end;
    emit 0
  end
end signal

```

- ▶ Can analyze this with just propagating *facts*
 - ▶ No need for speculative computation based on *assumptions*
 - ▶ Our analysis still “looks ahead” to see what must/cannot be done, but always builds on facts established so far, not on speculations
- ▶ However, analysis involves recomputations
 - ▶ **Avoiding this is goal of operational and circuit semantics!**

- ▶ We first start analyzing what the “signal S” statement must do with status \perp for 0. For this, we analyze its body with status \perp for 0 and S.
- ▶ We immediately find that S must be emitted since we must execute the “emit S” statement. Therefore, we redo the analysis with status \perp for 0 and + for S.
- ▶ We reach the test for 0. Since the status of 0 is unknown, there is nothing we must do and we can make progress only by analyzing what we cannot do in the branches of the test.
- ▶ In the then branch, there is a present test for S. Since S is known to be present, we cannot take the implicit else branch that would terminate. Since the then branch is a pause statement, it cannot terminate.
- ▶ Summing up things, the “present S” test cannot terminate. Therefore, the “emit 0” statement cannot be executed and 0 cannot be emitted. As a consequence we must set 0 absent and redo the analysis of the program with status $-$ for 0.
- ▶ We now find that we must take the implicit else branch of the “present 0” test that terminates execution.
- ▶ The program is constructive since we have fully determined the signal statuses.

Rejecting Programs

- ▶ If the must and cannot predicates bring no information about the status of some signal:
 - ▶ Programs is **rejected**

```

module P3:
  output 0;
  present 0 else emit 0 end
end module

```

```

module P4:
  output 0;
  present 0 then emit 0 end
end module

```

Note:

- ▶ The constructive semantics rejected P3 and P4 for the very *same* reason
- ▶ The logical behavioral semantics rejected P3 and P4 for two *different* reasons, namely non-reactivity and non-determinism

Rejecting Programs

- ▶ Constructiveness \implies logical correctness
- ▶ **But not vice versa!**

```

module P9:
[
  present 01 then emit 01 end
||
  present 01 then
    present 02 else emit 02 end
end
]

```

- ▶ Both 01 and 02 can be emitted
- ▶ No signal must be emitted
- ▶ No progress—**reject P9!**

Rejecting Programs

Consider variant of P2:

```

module P11:
signal S
  present 0 then
    emit S;
    present S then
      pause
    end;
    emit 0
  end
end signal

```

- ▶ Are not allowed to speculatively execute branches
- ▶ Again no progress—**reject P11!**

- ▶ The “emit S” statement is now inside the then branch of the “present 0” statement.
- ▶ The must analysis with status \perp for 0 and S finds nothing we must do since we are not allowed to speculatively compute within the branches of the test for 0.
- ▶ In the same status, the cannot analysis finds that both S and 0 can be emitted since it finds potentially reachable emitters.
- ▶ Therefore, we can make no progress and we reject P11.

Rejecting Programs

```

module P12:
  present 0 then
    emit 0;
  else
    emit 0
  end

```

- ▶ Must reject P12 as well!
- ▶ Does an equivalent HW-circuit always stabilize?
(Will come back to this later ...)

The *Must*, *Cannot*, and *Can* Functions

- ▶ *Cannot*^m function prunes out false paths
- ▶ $Cannot^m(p, E) = \langle Cannot_s^m(p, E), Cannot_k^m(p, E) \rangle = \langle S, K \rangle$
- ▶ Extra argument $m \in \{+, \perp\}$ indicates whether it is known that p must be executed in event E
- ▶ $Can^m(p, E)$ is component-wise complement

The *Must*, *Cannot*, and *Can* Functions

- ▶ *Must* function determines what must be done in a reaction
 $P \xrightarrow[\perp]{O} P'$
- ▶ Has the form $Must(p, E) = \langle S, K \rangle$
 - ▶ E : partial event, associating status in $B_{\perp} = \{+, -, \perp\}$ with each signal
 - ▶ S : set of signals that p must emit
 - ▶ K : set of completion codes that p must return
 - ▶ Is either empty or a singleton
- ▶ Use subscripts to access elements of result pair:
 - ▶ $Must(p, E) = \langle Must_s(p, E), Must_k(p, E) \rangle$

Definitions of *Must* and *Can*

- ▶ Completion and signal emission:

$$Must(k, E) = Can^m(k, E) = \langle \emptyset, \{k\} \rangle$$

$$Must(!s, E) = Can^m(!s, E) = \langle \{s\}, \{0\} \rangle$$

- ▶ Suspension:

$$Must(s \supset p, E) = Must(p, E)$$

$$Can^m(s \supset p, E) = Can^m(p, E)$$

Definitions of *Must* and *Can*

- ▶ Signal test:

$$Must((s? p, q), E) = \begin{cases} Must(p, E) & \text{if } s^+ \in E \\ Must(q, E) & \text{if } s^- \in E \\ \langle \emptyset, \emptyset \rangle & \text{if } s^\perp \in E \end{cases}$$

$$Can^m((s? p, q), E) = \begin{cases} Can^m(p, E) & \text{if } s^+ \in E \\ Can^m(q, E) & \text{if } s^- \in E \\ Can^\perp(p, E) \cup Can^\perp(q, E) & \text{if } s^\perp \in E \end{cases}$$

- ▶ Note that replacing $\langle \emptyset, \emptyset \rangle$ by $Must(p, E) \cap Must(q, E)$ would permit speculative execution
- ▶ This would accept for example `present 0 then emit 0 else emit 0 end`, where information flows backwards wrt. control.
- ▶ The physical analogy is that this would allow reasoning based on the law of excluded middle ($x \vee \neg x = 1$)—and electrons cannot perform this kind of reasoning (cf. unstable Hamlet circuit)

Definitions of *Must* and *Can*

- ▶ Sequencing:

$$Must(p; q, E) = \begin{cases} Must(p, E) & \\ \text{if } 0 \notin Must_k(p, E) & \\ \langle Must_S(p, E) \cup Must_S(q, E), Must_k(q, E) \rangle & \\ \text{if } 0 \in Must_k(p, E) & \end{cases}$$

$$Can^m(p; q, E) = \begin{cases} Can^m(p, E) & \\ \text{if } 0 \notin Can_k^m(p, E) & \\ \langle Can_S^m(p, E) \cup Can_S^{m'}(q, E), Can_k^m(p, E) \setminus 0 \cup Can_k^{m'}(q, E) \rangle & \\ \text{if } 0 \in Can_k^m(p, E) & \\ \text{with } m' = \begin{cases} + & \text{if } m = + \wedge 0 \in Must_k(p, E) \\ \perp & \text{otherwise} \end{cases} & \end{cases}$$

Definitions of *Must* and *Can*

- ▶ Local signal declaration:

$$Must(p \setminus s, E) = \begin{cases} Must(p, E * s^+) \setminus s & \text{if } s \in Must_S(p, E * s^\perp) \\ Must(p, E * s^-) \setminus s & \text{if } s \notin Can_S^+(p, E * s^\perp) \\ Must(p, E * s^\perp) \setminus s & \text{otherwise} \end{cases}$$

$$Can^m(p \setminus s, E) = \begin{cases} Can^+(p, E * s^+) \setminus s & \\ \text{if } m = + \text{ and } s \in Must_S(p, E * s^\perp) & \\ Can^m(p, E * s^-) \setminus s & \\ \text{if } s \notin Can_S^+(p, E * s^\perp) & \\ Can^m(p, E * s^\perp) \setminus s & \\ \text{otherwise} & \end{cases}$$

Definitions of *Must* and *Can*

- ▶ Note the *Can/Must* asymmetry: in the *Can*-predicate of the local signal declaration, check for $m = +$ before calling *Must* to avoid speculative computation
- ▶ Otherwise, would accept program

```

present 0 then
  signal S in
    emit S
  ||
  present S else emit 0 end
end
end

```

- ▶ Would accept program on the following grounds: since the body of the signal statement must emit S, the output 0 cannot be emitted and can be set absent.
- ▶ This reasoning speculatively executes the `emit S` statement.

Definitions of *Must* and *Can*

- ▶ Loop:

$$Must(p^*, E) = Must(p, E)$$

$$Can^m(p^*, E) = Can^m(p, E)$$

- ▶ Parallel:

$$Must(p|q, E) = \langle Must_S(p, E) \cup Must_S(q, E), \\ Max(Must_k(p, E), Must_k(q, E)) \rangle$$

$$Can^m(p|q, E) = \langle Can_S^m(p, E) \cup Can_S^m(q, E), \\ Max(Can_k^m(p, E), Can_k^m(q, E)) \rangle$$

The *Max*-operator on sets of completion codes is defined as

$$Max(K, L) = \begin{cases} \emptyset & \text{if } K = \emptyset \text{ or } L = \emptyset \\ \{\max(k, l) \mid k \in K, l \in L\} & \text{if } K, L \neq \emptyset \end{cases}$$

Definitions of *Must* and *Can*

- ▶ Trap:

$$Must(\{p\}, E) = \langle Must_S(p, E), \downarrow Must_k(p, E) \rangle$$

$$Can^m(\{p\}, E) = \langle Can_S^m(p, E), \downarrow Can_k^m(p, E) \rangle$$

- ▶ Shift:

$$Must(\uparrow p, E) = \langle Must_S(p, E), \uparrow Must_k(p, E) \rangle$$

$$Can^m(\uparrow p, E) = \langle Can_S^m(p, E), \uparrow Can_k^m(p, E) \rangle$$

Definition of the Constructive Behavioral Semantics

The **constructive behavioral semantics** of a given program is defined by a two-step procedure, yielding the current reaction and the derivative:

1. Compute output event O using *Must* and *Cannot* predicates
 - ▶ This fails if status of some output signal cannot be determined to be $+$ or $-$
2. Compute behavioral transition yielding program derivative
 - ▶ This fails if body of some loop is found to terminate instantaneously
 - ▶ This also fails if we cannot establish the presence/absence of a local signal

Definition of the Constructive Semantics

Step 1: Compute output event O

Approach:

- ▶ Start with undefined O (all output signal statuses = \perp)
- ▶ Iteratively enrich O using *Must* and *Can* information
- ▶ Terminate when this stabilizes (guaranteed by monotonicity)

Formalize this as computation of a least fixed point (see draft book)

Algorithm to Compute Outputs

```
function computeOut(P, I)
  E = I ∪ {s⊥ | s ∈ Out(P)}
  do
    E' = E
    can = CanS+(P, E)
    must = MustS(P, E)
    E = I ∪ {s+ | s ∈ must}
      ∪ {s- | s ∈ Out(P) \ can}
      ∪ {s⊥ | s ∈ can \ must}
  while (E' ≠ E)
  if ∃s : s⊥ ∈ E then error ("not constructive")
  return E
```

- ▶ I is an input event, which maps $+$, $-$ to all input signals
- ▶ $In(P)$ and $Out(P)$ give the input and output signals of an program P .

Example for *Can* analysis

Consider the program $p = !S; S?!O, 1$ and environment $\{S^\perp, O^\perp\}$.

$$\begin{aligned} Can^+(!S, \{S^\perp, O^\perp\}) &= \langle \{S\}, \{0\} \rangle \\ Must_k(!S, \{S^\perp, O^\perp\}) &= \{0\} \\ Can^+(!O, \{S^\perp, O^\perp\}) &= \langle \{O\}, \{0\} \rangle \\ Can^+(1, \{S^\perp, O^\perp\}) &= \langle \emptyset, \{1\} \rangle \\ Can^+(S?!O, 1, \{S^\perp, O^\perp\}) &= \langle \{O\}, \{0, 1\} \rangle \\ Can^+(!S; S?!O, 1, \{S^\perp, O^\perp\}) &= \langle \{S, O\}, \{0, 1\} \rangle \end{aligned}$$

Gives no new information on signal status

The *Must* analysis in the third line is needed to determine the correct status for the *Can* analysis.

Example for *Must* analysis

Consider the program $p = !S; S?!O, 1$ and environment $\{S^\perp, O^\perp\}$

1. $Must(!S, \{S^\perp, O^\perp\}) = \langle \{S\}, \{0\} \rangle$
 $Must(S?!O, 1, \{S^\perp, O^\perp\}) = \langle \emptyset, \emptyset \rangle$
 $Must(!S; S?!O, 1, \{S^\perp, O^\perp\}) = \langle \{S\}, \emptyset \rangle$
2. Update environment to $\{S^+, O^\perp\}$
3. $Must(!S, \{S^+, O^\perp\}) = \langle \{S\}, \{0\} \rangle$
 $Must(!O, \{S^+, O^\perp\}) = \langle \{O\}, \{0\} \rangle$
 $Must(S?!O, 1, \{S^+, O^\perp\}) = \langle \{O\}, \{0\} \rangle$
 $Must(!S; S?!O, 1, \{S^+, O^\perp\}) = \langle \{S, O\}, \{0\} \rangle$
4. Update environment to $\{S^+, O^+\}$
5. All signals have a defined status \rightarrow done

In the third step, we could first perform a *Can* analysis, but this would not give new information in this example.

Definition of the Constructive Semantics

Step 2: Compute transition

Rules are exactly as for logical behavioral semantics—except for changed rules for local signals

$$\frac{p \xrightarrow[E*s^+]{E'*s^+,k} p' \quad S(E') = S(E) \setminus s}{p \setminus s \xrightarrow[E]{E',k} p' \setminus s} \quad (\text{sig } +)$$

is replaced with

$$\frac{s \in \text{Must}_s(p, E * s^\perp) \quad p \xrightarrow[E*s^+]{E'*s^+,k} p' \quad S(E') = S(E) \setminus s}{p \setminus s \xrightarrow[E]{E',k} p' \setminus s} \quad (\text{csig } +)$$

The Constructive Operational Semantics

- ▶ ... is defined by a rewriting-based interpretation scheme
 - ☺ Instead of reasoning about what we must do, just do it
 - ☹ Formal definition and technical treatment of the constructive *operational* semantics is much heavier than that of the constructive *behavioral* semantics
- ▶ Will still take constructive *behavioral* semantics as the primary semantics

Definition of the Constructive Semantics

$$\frac{p \xrightarrow[E*s^-]{E'*s^-,k} p' \quad S(E') = S(E) \setminus s}{p \setminus s \xrightarrow[E]{E',k} p' \setminus s} \quad (\text{sig } -)$$

is replaced with

$$\frac{s \in \text{Cannot}_s^+(p, E * s^\perp) \quad p \xrightarrow[E*s^-]{E'*s^-,k} p' \quad S(E') = S(E) \setminus s}{p \setminus s \xrightarrow[E]{E',k} p' \setminus s} \quad (\text{csig } -)$$

The Constructive Operational Semantics

- ▶ Decorate signal declarations with status +, -, \perp
- ▶ Initially, all signals except inputs unknown
- ▶ Constructive operational semantics is a **micro-step semantics**
 - ▶ Current state indicated by •

The Constructive Operational Semantics

Consider P1 with I present:

```

module P1:
input I+;
output O⊥;
•signal S1⊥, S2⊥ in
  present I then emit S1 end
||
  present S1 else emit S2 end
||
  present S2 then emit O end
end signal
end module

```

The Constructive Operational Semantics

Only first thread can continue:

```

module P1:
input I+;
output O⊥;
signal S1⊥, S2⊥ in
  present I then •emit S1 end
||
  •present S1 else emit S2 end
||
  •present S2 then emit O end
end signal
end module

```

The Constructive Operational Semantics

Fork of the parallel statement:

```

module P1:
input I+;
output O⊥;
signal S1⊥, S2⊥ in
  •present I then emit S1 end
||
  •present S1 else emit S2 end
||
  •present S2 then emit O end
end signal
end module

```

When encountering a “present S” statement in a thread:

- ▶ If S is annotated with +, we transfer control to the then branch.
- ▶ If S is annotated with −, we transfer control to the else branch.
- ▶ If S is annotated by ⊥, we block until the status of S becomes + or −

The Constructive Operational Semantics

Now emit S1:

```

module P1:
input I+;
output O+;
signal S1+, S2+ in
  present I then emit S1 end•
||
  •present S1 else emit S2 end•
||
  •present S2 then emit 0 end
end signal
end module

```

The Constructive Operational Semantics

Cannot emit S2 any more:

```

module P1:
input I+;
output O+;
signal S1+, S2- in
  present I then emit S1 end•
||
  present S1 else emit S2 end•
||
  •present S2 then emit 0 end
end signal
end module

```

The Constructive Operational Semantics

Now the 2nd branch can continue:

```

module P1:
input I+;
output O+;
signal S1+, S2+ in
  present I then emit S1 end•
||
  present S1 else emit S2 end•
||
  •present S2 then emit 0 end
end signal
end module

```

The Constructive Operational Semantics

Now 3rd branch can continue:

```

module P1:
input I+;
output O+;
signal S1+, S2- in
  present I then emit S1 end•
||
  present S1 else emit S2 end•
||
  present S2 then emit 0 end•
end signal
end module

```

The Constructive Operational Semantics

Cannot emit 0 any more:

```

module P1:
input I+;
output O-;
signal S1+, S2- in
  present I then emit S1 end•
||
  present S1 else emit S2 end•
||
  present S2 then emit 0 end•
end signal
end module

```

The Constructive Operational Semantics

Now consider P2:

```

module P2:
output O+;
•signal S+ in
  emit S;
  present 0 then
    present S then
      pause
    end;
    emit 0
  end
end signal
end module

```

The Constructive Operational Semantics

Synchronize the terminated threads:

```

module P1:
input I+;
output O-;
signal S1+, S2- in
  present I then emit S1 end
||
  present S1 else emit S2 end
||
  present S2 then emit 0 end
end signal•
end module

```

The Constructive Operational Semantics

After 3 microsteps:

```

module P2:
output O+;
signal S+ in
  emit S;
  •present 0 then
    present S then
      pause
    end;
    emit 0
  end
end signal
end module

```


The Constructive Operational Semantics

Perform cannot analysis (as in constructive behavioral semantics)—and set 0 absent:

```

module P2:
  output O-;
  signal S+ in
  emit S;
  •present 0 then
    present S then
      pause
    end;
    emit 0
  end
end signal
end module

```

The Constructive Operational Semantics

- ▶ Statuses evolve monotonically
 - ▶ Hence avoid most of the recomputations that take place in the constructive behavioral semantics
- ▶ Rejecting programs is similar to constructive behavioral semantics

```

module P3:
  output 0;
  present 0 else emit 0 end
end module

```

- ▶ No possible initial microstep \implies cannot set O^+
- ▶ Potential path to emit 0 \implies cannot set O^-

The Constructive Operational Semantics

Take implicit else branch of test:

```

module P2:
  output O-;
  signal S+ in
  emit S;
  present 0 then
    present S then
      pause
    end;
    emit 0
  end
end signal•
end module

```

Summary of Constructive Interpretation

Signals:

- ▶ Signals are shared objects with status $\{+, -, \perp\}$
- ▶ Signal status initialization:
 - ▶ Input signals are initialized according to the input event
 - ▶ Other signals initialized to \perp
- ▶ Signal status changes:
 - ▶ Status of a signal S changes from \perp to $+$ as soon as an “emit S ” statement is executed
 - ▶ Status of a signal S changes from \perp to $-$ as soon as all the “emit S ” statements have been found unreachable by the cannot false path analysis

Summary of Constructive Interpretation

Control:

- ▶ Sequential threads of control forked by parallel statements
- ▶ When a thread reaches a “present S ” statement:
 - ▶ As long as the status of S is \perp :
 - ▶ Control remains there, frozen,
 - ▶ As soon as S has a non- \perp status:
 - ▶ Control can resume
- ▶ If several threads are enabled, any one of them can be chosen

Summary of Constructive Interpretation

Control:

- ▶ Threads are stopped by termination or by executing pause or exit statements
- ▶ Parallel statements synchronize stopped threads, as explained in the intuitive semantics
- ▶ Finally, the false path analysis explores all possible instantaneous paths towards emit statements
 - ▶ Takes into account all facts established so far
 - ▶ No speculative reasoning

Summary of Constructive Interpretation

Program Acceptance:

- ▶ Given an input, a program is accepted if the analysis succeeds in setting each signal status to a defined value + or –
- ▶ Logical correctness is guaranteed for accepted programs

To Go Further

- ▶ Albert Benveniste, Paul Caspi, Stephen A. Edwards, Nicolas Halbwachs, Paul Le Guernic, Robert De Simone, The synchronous languages 12 years later, *Proceedings of the IEEE*, Jan. 2003 vol. 91, issue 1, pages 64–83, <http://citeseerx.ist.psu.edu/viewdoc/summary?doi=10.1.1.96.1117>