Synchronous Languages—Lecture 05

Prof. Dr. Reinhard von Hanxleden

Christian-Albrechts Universität Kiel Department of Computer Science Real-Time Systems and Embedded Systems Group

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Esterel III—The Logical Semantics

The 5-Minute Review Session

- 1. How do concurrent threads in Esterel communicate?
- 2. What is the difference between weak and strong abortion?
- 3. What is the difference between *aborts* and *traps*?
- 4. What is syntactic sugar, and what is it good for?
- 5. What is the multiform notion of time?

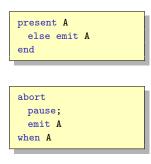


Causality issues The logical coherence law Logical reactivity and determinism Instantaneous Feedback

The Logical Behavioral Semantics



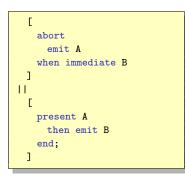
Causality Problems



present A	
then pause	
end;	
emit A	

- It's easy to write contradictory programs
- Unfortunate side-effect of instantaneous communication coupled with the single valued signal rule
- These sorts of programs are erroneous and flagged by the Esterel compiler as incorrect
- Note: the first and third example are considered valid in SCEst, see later

Causality Problems



Can be very complicated because of instantaneous communication



Causality

- Definition has evolved since first version of the language
- Original compiler had concept of "potentials"
 - Static concept: at a particular program point, which signals could be emitted along any path from that point
- Current definition based on "constructive causality"
 - Dynamic concept: whether there's a "guess-free proof" that concludes a signal is absent

Causality Example



Analysis done by original compiler:

- After emit A runs, there's a static path to emit B
- Therefore, the value of B cannot be decided yet
- Execution procedure deadlocks: Program is bad

Causality Example



Analysis done by later compilers:

- After emit A runs, it is clear that B cannot be emitted because A's presence runs the "then" branch of the second present
- B declared absent, both present statements run
- Program is OK

- The intuitive semantics:
 - Specifies what should happen when executing a program
- However, also want to guarantee that
 - Execution actually exists (at *least* one possible execution)
 - Execution is unique (at most one possible execution)
- Need extra criteria for this!
- The apparently simplest possible criterion: logical correctness

Recall:

- Signal S is absent by default
- Signal S is present if an emit S statement is executed

The Logical Coherence Law:

A signal S is present in a tick if and only if an *emit S* statement is executed in this tick.

Logical Correctness requires:

There exists exactly one status for each signal that respects the coherence law

Given:

- Program P and input event I
- *P* is logically reactive w.r.t. *I*:
 - There is at least one logically coherent global status
- *P* is logically deterministic w. r. t. *I*:
 - There is at most one logically coherent global status
- *P* is logically correct w.r.t. *I*:
 - P is both logically reactive and deterministic

P is logically correct:

- P is logically correct w.r.t. all possible input events
- Is logical correctness decidable?
 - Yes!

```
module P1:
input I;
output 0;
signal S1, S2 in
present I then emit S1 end
||
present S1 else emit S2 end
||
present S2 then emit 0 end
end signal
end module
```

Is P1 logically correct?
 Yes!

```
module P2:
signal S in
emit S;
present 0 then
present S then
pause
end;
emit 0
end
end signal
```

Is P2 logically correct?

Yes!

- Notice that P2 is inputless
- Inputless programs react on empty input events, *i. e.*, on clock ticks

module P3:
present O else emit O end
end module

module P4: present 0 emit 0 end end module

module P5:
present 01 then emit 02 end
||
present 02 else emit 01 end

Is P3 logically correct?

No!

- This is non-reactive
- Is P4 logically correct?
 - ► No!
 - This is nondeterministic

Is P5 logically correct?

► No!

This is non-reactive

module P6:
present 01 then emit 02 end
||
present 02 then emit 01 end

Is P6 logically correct?

- ► No!
- This is nondeterministic

module P7:
present 0 then pause end;
emit 0

Is P7 logically correct?

- ► No!
- This is non-reactive

```
module P8:
trap T in
    present I else pause end;
    emit 0
||
    present 0 then exit T end
end trap;
emit 0
```

Is this logically correct?

- Yes for I present
- Nondeterministic for I absent

```
module P9:
[
   present 01 then emit 01 end
]
   present 01 then
   present 02 else emit 02 end
   end
]
```

Is P9 logically correct?

Yes

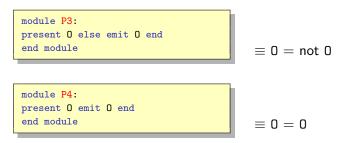
 Note that this contains the nondeterministic program P4 and the non-reactive program P3!

Instantaneous Feedback

Want to reject logically incorrect programs at compile time

One option:

- Forbid static self-dependency of signals
- Similar to acyclicity requirement for electrical circuits
- This is what the Esterel v4 compiler did



Instantaneous Feedback

However, forbidding cycles would also reject the following:

```
module GoodCycle1:
present I then
present 01 then emit 02 end
else
present 02 then emit 01 end
end present
```

- O1 and O2 cyclically depend on each other
- However, any given status of I breaks the cycle

Instantaneous Feedback

```
module GoodCycle2:
present 01 then emit 02 end;
pause;
present 02 then emit 01 end
```

- Here the cycle is neutralized with a delay
- In general, requiring acyclicity turns out to be inadequate to Esterel practice

Logical Correctness—Assessment

- We now introduced logical correctness
- But do we want to use it as basis for the language?
 - sound
 - © sometimes unintuitive (consider P9)
 - © computationally complex
- Alternative 1: allow only programs that are acyclic
 - ③ simple
 - S too restrictive (consider GoodCycle1/2)
- Alternative 2: accept everything for which the compiler finds a static execution schedule
 - $\ensuremath{\textcircled{}}$ relatively simple for the compiler
 - definition not precise, depends on abilities of compiler (different compilers accept different programs)
- Alternative 3: the constructive semantics
 - 🙂 analysis not trivial
 - clear semantics



The Logical Behavioral Semantics Notation and Definitions The Basic Broadcasting Calculus Transition Rules Reactivity and Determinism

The Semantics of Esterel

- 1. Logical Behavioral Semantics
 - Rewriting rules defining reactivity, determinism, and logical correctness
 - Signal coherence law embedded in rules for local signals
- 2. Constructive Behavioral Semantics
 - Refines logical behavioral semantics
 - Based on must and cannot analysis
- 3. Logical/Constructive State Behavioral Semantics
 - Replaces rewriting with marking of active delays (v5 debugger)
- 4. Constructive State Operational Semantics
 - Defines reaction as sequence of microsteps (v3 compiler)
- 5. Constructive Circuit Semantics
 - Translates Esterel programs into Boolean digital circuits (v5 compiler)

- Sort S: A set of signals
- Signal statuses: $B = \{+,-\}$
- Event *E*:
 - Given sort S, defines status $E(s) \in B$ for each $s \in S$
 - Obtain sort of E as S(E) = S
- Two equivalent representations for E:
 - As subset of S: $E = \{s \in S \mid E(s) = +\}$
 - As a mapping from S to B: $E = \{(s, b) \mid b = E(s)\}$

- Write $s^+ \in E$ iff E(s) = +
- Write $s^- \in E$ iff E(s) = -
- ▶ Write $E' \subset E$ iff $\forall s \in S(E') : s^+ \in E' \implies s^+ \in E$
- Given signal *s*, define singleton event $\{s^+\}$:

•
$$\{s+\}(s) = +$$

• $\forall s' \neq s : \{s+\}(s') = -$

• Given signal set S and signal $s \in S$, write $S \setminus s = S - \{s\}$

Given E and s ∈ S(E), write E \ s to denote event of sort S(E) \ s, which coincides with E on all signals but s

• Define
$$E * s^b$$
 as event E' of sort $S(E) \cup \{s\}$ with

•
$$E'(s) = b$$
, $E'(s') = E(s')$ for $s' \neq s$

- Will present formal semantics as Plotkin's Structural Operational Semantics (SOS) inference rules
- Behavioral Semantics formalizes reaction of program P as behavioral transition

$$P \xrightarrow[l]{O} P'$$

- I: input event
- O: output event
- P': derivative of P—the program for the next instance

Auxiliary statement transition relation:

$$p \xrightarrow{E',k} p'$$

- p: program body (of P)
- E: event defining status of all signals declared in scope of p
- \blacktriangleright E': event composed of all signals emitted by p in the reaction
- \blacktriangleright k: completion code returned by p (0 iff p terminates)
- p': derivative of p
- Logical coherence (or broadcasting invariant):

$$E' \subset E$$



- Program P with body p
- Input event I

Define program transition of P by statement transition of p:

$$P \xrightarrow[l]{O} P'$$
 iff $p \xrightarrow[l\cup O]{O,k} p'$ for some k

These program transitions, yielding an output reaction O and a derivative P', determine the logical behavioral semantics of P

The Basic Broadcasting Calculus

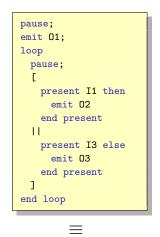
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- For concise presentation of rules: Replace Esterel syntax with terser process-calculus syntax
- Use parenthesis for grouping statements

nothing	0
pause	1
emit s	<u>!</u> s
present s then p else c	q end s?p,q
p; q	p; q
loop p end	p*
$p \parallel q$	pq
signal s in p end	p \ s
suspend p when s end	s ⊃ p
trap T in p end	{ <i>p</i> }
exit T	$\frac{k}{k}$ with $k \ge 2$
[no concrete syntax]	↑ <i>p</i>
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Example



1; !O1; (1; ((17 !O2, 0) | (13 ? 0, !O3)))*

Basic Transition Rules

The null process 0:

The unit delay process 1:

Signal emission:

$$0 \xrightarrow[E]{\emptyset,0} 0$$

$$1 \xrightarrow[E]{\emptyset,1} 0$$

$$!s \xrightarrow{\{s\},0} 0$$



(unit delay)

(emit)

Deduction Rules

In addition to simple transition rules, will also use deduction rules

Hypothesis: If sub-instructions behave like this

$$\frac{p_1 \xrightarrow{E'_1, k_1}{E} p'_1 \quad p_2 \xrightarrow{E'_2, k_2}{E} p'_2 \quad \text{Other hypotheses}}{\text{Instruction}(p_1, p_2) \xrightarrow{E'(E'_1, E'_2) \quad \mathcal{K}(k_1, k_2)}{E} \text{Instruction}'(p'_1, p'_2)}$$

 Conclusion: ... then the compound instruction behaves like that

Deduction Rules—Sequencing

$$\frac{p \xrightarrow{E',k} p' \quad k \neq 0}{p; q \xrightarrow{E',k} p'; q}$$



$$\frac{p \xrightarrow{E'_{\rho}, 0} p' \quad q \xrightarrow{E'_{q}, k} q'}{\frac{p; q \xrightarrow{E'_{\rho} \cup E'_{q}, k}}{E} q'}$$



Deduction Rules—Looping and Parallel

$$\frac{p \xrightarrow{E',k} p' \quad k \neq 0}{p^* \xrightarrow{E',k} p'; (p^*)}$$



$$\boxed{\frac{p \xrightarrow{E_{p}',k} p' \quad q \xrightarrow{E_{q}',l} q'}{p|q \xrightarrow{E_{p}' \cup E_{q}',\max(k,l)} p'|q'}}$$

Deduction Rules—Conditional

$$\frac{s^+ \in E \quad p \xrightarrow{E',k} p'}{s?p,q \xrightarrow{E',k} p'}$$

$$\frac{s^{-} \in E \quad q \xrightarrow{E',k} q'}{s?p,q \xrightarrow{E',k} q'}$$

Zero delay: can use decision trees to test for arbitrary Boolean conditions:

Deduction Rules—Restriction

$$\frac{p \xrightarrow{E' * s^+, k} p' \quad S(E') = S(E) \setminus s}{p \setminus s \xrightarrow{E', k} p' \setminus s}$$

$$(sig +)$$

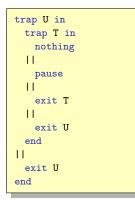
(sig -)

$$\frac{p \xrightarrow{E' * s^-, k} p' \quad S(E') = S(E) \setminus s}{p \setminus s \xrightarrow{E', k} p' \setminus s}$$

Note: This also properly handles nested restrictions of the same signal

Traps—Example

- The trap exit encoding is
 - k = 2 if the closest enclosing trap is exited, and
 - k = n + 2 if *n* trap declarations have to be traversed



 $\equiv \ \{\{0 \mid 1 \mid 2 \mid 3\} \mid 2\}$

Two Operators on Completion Codes

The ↓k operator computes completion code of {p} from that of p:

$$\downarrow k = 0 \qquad \text{if } k = 0 \quad \text{or } k = 2$$

$$\downarrow k = 1 \qquad \text{if } k = 1$$

$$\downarrow k = k - 1 \quad \text{if } k > 2$$

The ↑k operator computes completion code of ↑p from that of p; want {↑p} ≡ p

The Shift Operator

- ► May use ↑ in definitions of derived operators

```
suspend p when immediate ss \cdot \supset p\equiv \{(s?1,2)^*\}; s \supset pawait immediate s; ps \cdot \Rightarrow p\equiv \{(s?(\uparrow p; 2), 1)^*\}await s; ps \Rightarrow p\equiv 1; s \cdot \Rightarrow pweak abort p when immediate ss \cdot > p\equiv \{(\uparrow p; 2) \mid s \cdot \Rightarrow 2\}weak abort p when immediate ss > p\equiv \{(\uparrow p; 2) \mid s \cdot \Rightarrow 2\}abort p when immediate ss \cdot \gg p\equiv s \cdot > (s \cdot \supset p)abort p when ss \gg p\equiv s \cdot > (s \cup p)
```

Traps—The Rules

$$\frac{k \stackrel{\emptyset,k}{E} 0}{E} 0 \qquad (exit)$$

$$\frac{p \stackrel{E',k}{E} p' \quad k = 0 \text{ or } k = 2}{\{p\} \stackrel{E',0}{E} 0} \qquad (trap1)$$

$$\frac{p \stackrel{E',k}{E} p' \quad k = 1 \text{ or } k > 2}{\{p\} \stackrel{E',\downarrow k}{E} \{p'\}} \qquad (trap2)$$

$$\frac{p \stackrel{E',k}{E} p'}{\uparrow p \stackrel{E',\uparrow k}{E} \uparrow p'} \qquad (shift)$$

Deduction Rules—Suspension

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$$\frac{p \xrightarrow{E',0} p'}{s \supset p \xrightarrow{E',0} 0}$$

(suspend1)

$$\frac{p \xrightarrow{E',k} p' \quad k \neq 0}{s \supset p \xrightarrow{E',k} s \cdot \supset p'}$$

(suspend2)

Reactivity and Determinism

- ▶ Definition: Program P is logically reactive (resp. logically deterministic) w.r.t. an input event I if there exists at least (resp. at most) one program transition P ⊖/I P' for some output event O and program derivative P'
- Definition: Program P is logically correct if it is logically reactive and logically deterministic
- ▶ How about (*s*?!*s*, 0)?
- And how about (s?0, !s)?

Reactivity and Determinism

- I/O determinism still leaves room for internal non-determinism
 - ► Consider (s?!s, 0) \ s
 - Forbidden in constructive semantics
- Definition: Program P is strongly deterministic for an input event *I* iff
 - P is reactive and deterministic for this event, and
 - there exists a unique proof of the unique transition $P \xrightarrow{O} P'$.

Summary (1/3)

- The intuitive semantics specifies what should happen when executing a program
- However, also want to guarantee that exactly one possible execution exists that satisfies the intuitive semantics
- The Logical Coherence Law specifies that a signal S is present in a tick if and only if an "emit S" statement is executed in this tick
- Logical Correctness requires that there exists exactly one status for each signal that respects the coherence law

Summary (2/3)

- P is logically reactive w.r.t. input I if there is at least one logically coherent global status
- P is logically deterministic w. r. t. I if there is at most one logically coherent global status
- P is logically correct w.r.t. I if P is both logically reactive and deterministic
- P is logically correct if P is logically correct w.r.t. all possible input events

Summary (3/3)

- There exist several semantics for the Esterel language—one important distinction is between *logical* and *constructive* semantics, the latter being a refinement of the former
- We started discussing the logical behavioral semantics, expressed in Plotkin's Structural Operational Semantics, with basic transition rules and deduction rules
- We formally defined reactivity, determinism, logical correctness, and strong determinism

To Go Further

- Gérard Berry, The Constructive Semantics of Pure Esterel, Draft book, current version 3.0, Dec. 2002 http://www-sop.inria.fr/members/Gerard.Berry/ Papers/EsterelConstructiveBook.zip
- Gérard Berry, Preemption in Concurrent Systems, In Proceedings FSTTCS 93, Lecture Notes in Computer Science 761, pages 72-93, Springer-Verlag, 1993, http://citeseerx.ist.psu.edu/viewdoc/summary?doi= 10.1.1.42.1557