Synchronous Languages—Lecture 14

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Sequentially Constructive Concurrency in Practice

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- 2. What is confluence in the SC MoC?
- 3. What is thread reincarnation?
- 4. In the SC MoC, when are threads considered *statically concurrent*?
- 5. What is a *thread tree*? How can it be used to define static concurrency?

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- 1. How is *run-time concurrency* defined? How does it relate to static concurrency?
- 2. What is *SC-admissibility*?
- 3. When is a program sequentially constructive?
- 4. What is an SC-schedule? When is it valid?
- 5. What are conservative, practical approximations of sequential constructiveness?

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References

Most of the material here draws from this reference [TECS]:



R. von Hanxleden, M. Mendler, J. Aguado, B. Duderstadt, I. Fuhrmann, C. Motika, S. Mercer, O. O'Brien, and P. Roop.

Sequentially Constructive Concurrency – A Conservative Extension of the Synchronous Model of Computation.

ACM Transactions on Embedded Computing Systems, Special Issue on Applications of Concurrency to System Design, July 2014, 13(4s). http://rtsys.informatik.uni-kiel.de/~biblio/downloads/papers/tecs14.pdf

Unless otherwise noted, the numberings of definitions, sections etc. refer to this.

There is also an extended version [TR]:



R. von Hanxleden, M. Mendler, J. Aguado, B. Duderstadt, I. Fuhrmann, C. Motika, S. Mercer, O. O'Brien, and P. Roop.

Sequentially Constructive Concurrency – A Conservative Extension of the Synchronous Model of Computation.

Christian-Albrechts-Universität zu Kiel, Department of Computer Science, Technical Report 1308, ISSN 2192-6247, Aug. 2013, 13(4s). http://rtsys.informatik.uni-kiel.de/~biblio/downloads/

http://rtsys.informatik.uni-kiel.de/~biblio/downloads/papers/report-1308.pdf

SC-Schedules
Schedule Order
Schedule / Program Classe

Overview

Conservative Static Approximation of SC

SC-Schedules

Schedule Order

Schedule / Program Classes

Determining SC-Schedules with Priorities

Summary

In practice, a compiler must be conservative:

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- May not recognize confluence
- May not recognize that writes are relative

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 - ▶ for every macro tick *R* of *G* which can be reached and executed under the SC-admissibility rules,
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Lemma: E_{ins} is valid

- Given: Valid SC-schedule Σ
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However: valid schedule may still contain conflicting orderings that cannot be satisfied or where it depends on the capabilities of the compiler or the run-time system whether it can be implemented

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Program (SCG) properties

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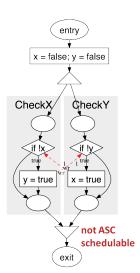
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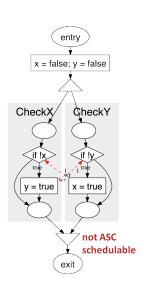
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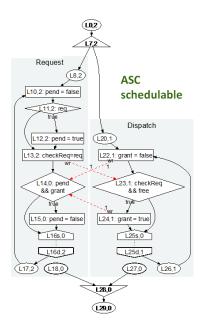
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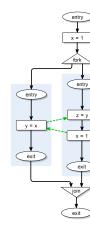
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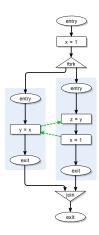
May also relax the sequential order to only order non-confluent statements → data-flow acyclic programs



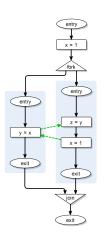


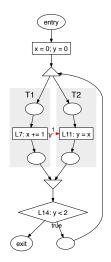




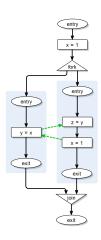


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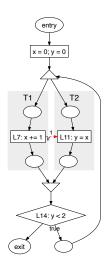




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Overview

Conservative Static Approximation of SC

Determining SC-Schedules with Priorities Priority-Based Scheduling [Sec. 5.2] Computing Priorities [Sec. 5.3]

Summary

Priorities [Def. 5.6, Lemma 5.7]

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- ▶ Priority n.pr of statement $n \in N$: maximal number of \rightarrow_{iur} edges traversed by any path in Σ that originates in n

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Lemma: Priorities implement the schedule order Given:

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- ▶ For example $n_1 \rightarrow_{iu} n_2$ implies $n_1 \rightarrow_{iur} n_2$, which implies, by definition of priorities, $n_1.pr > n_2.pr$, which in turn implies that n_1 gets scheduled before n_2

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Theorem

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Theorem

A program is IASC iff there exists a valid SC-schedule such that all statement priorities are finite



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- ► For arbitrary (*i. e.*, possibly cyclic) weighted graphs, the computation of the longest weighted path is NP-hard
- However, can exclude all graphs with a positive weight cycle

Detect whether Σ has a positive weight cycle.
 We can do so by computing the Strongly Connected
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 checking if any SCC contains a node that is connected to
 another node within the same SCC by a →_{iur} edge.
- If a positive weight cycle exists, then Σ is not *iur*-acyclic; we then **reject** the program.
 Otherwise, we **accept** the program, and continue.
 Now nodes in the same SCC can reach each other, but only through paths with weight 0, and therefore must have the same priority.

3. From the SCCs, construct the directed acyclic graph $G_{SCC} = (N_{SCC}, E_{SCC})$, where $N_{SCC} \subset N$ contains a representative node from each SCC of G (using e.g. the SCC roots computed by Tarjan's algorithm), and E_{SCC} contains an edge from one SCC representative to another iff the corresponding SCCs are connected in G. Here we assign an edge in E_{SCC} the maximum weight of the corresponding edges in Σ .

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Complexity:

- 3. From the SCCs, construct the directed acyclic graph $G_{SCC} = (N_{SCC}, E_{SCC})$, where $N_{SCC} \subset N$ contains a representative node from each SCC of G (using e.g. the SCC roots computed by Tarjan's algorithm), and E_{SCC} contains an edge from one SCC representative to another iff the corresponding SCCs are connected in G. Here we assign an edge in E_{SCC} the maximum weight of the corresponding edges in Σ .
- 4. Compute for each $n_{SCC} \in N_{SCC}$ the maximum weighted length (priority) $n_{SCC}.pr$ of any path originating in n_{SCC} , e. g., with a depth-first recursive traversal of all edges in the acyclic G_{SCC} .
- 5. Assign each statement $n \in N$ the priority computed for its SCC.

Complexity: linear in size of SCG

Overview

Conservative Static Approximation of SC

Determining SC-Schedules with Priorities

Summary

Summary I

Underlying idea of sequential constructiveness rather simple

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However, precise definition of SC MoC not trivial

- Challenging to ensure conservativeness relative to Berry-constructiveness
- Plain initialize-update-read protocol does not accommodate, e. g., signal re-emissions
- Restricting attention to concurrent, non-confluent node instances is key

Slide 19

Summary II

ASC-schedulability

- Is conservative approximation to SC
- Basis for practical implementation

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ASC-schedulability

- Is conservative approximation to SC
- ▶ Basis for practical implementation

Future work

- ▶ Plenty of it (SC+, optimized code gen, improved SCCharts transformations, . . .)
- Talk to us if you want to be part of it