C, Java vs. Synchronous Programming The Control Example A Constructive Game of Schedulability

Synchronous Languages—Lecture 13

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Lecture 13



Synchronous Languages

Safety-Critical Embedded Systems

Wran-U



- Embedded systems often safety-critical
- Safety-critical systems must react deterministically
- Computations often exploit concurrency
- ► Key challenge: Concurrency must be deterministic!

Thanks to Michael Mendler (U Bamberg) for support with these slides

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Motivation		Motivation	C, Java vs. Synchronous Programming
Formalizing Sequential Constructiveness (SC)		Formalizing Sequential Constructiveness (SC)	The Control Example
Wrap-Up		Wrap-Up	A Constructive Game of Schedulability
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Slide 1

The 5-Minute Review Session

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- 1. How do SCCharts and SyncCharts differ?
- 2. What does the initialize-update-read protocol refer to?
- 3. What is the SCG?
- 4. What are basic blocks? What are scheduling blocks?
- 5. When compiling from the SCG, what types of *low-level* synthesis do we distinguish? How do they compare?

Implementing (Deterministic) Concurrency

- ► C. Java. etc.:
 - © Familiar
 - © Expressive sequential paradigm
 - © Concurrent threads unpredictable in functionality and timing

Synchronous Programming:

- © predictable by construction
 - \implies Constructiveness
- © Unfamiliar to most programmers
- © Restrictive in practice

Aim: Deterministic concurrency with synchronous foundations, but without synchronous restrictions.

Motivation Formalizing Sequential Constructiveness (SC) Wrap-Up	C, Java vs. Synchronous Programming The Control Example A Constructive Game of Schedulability	Motivation C, Java vs. Synchronous Programming Formalizing Sequential Constructiveness (SC) The Control Example Wrap-Up A Constructive Game of Schedulability
Comparing Both Worlds		Implementing Deterministic Concurrency: SC MoC
 Sequential Languages C, Java, Asynchronous schedule By default: Multiple concurrent readers/writers On demand: Single assignment synchronization (locks, semaphores) Imperative All sequential control flow prescriptive Resolved by programmer 	 Synchronous Languages Esterel, Lustre, Signal, SCADE, SyncCharts Clocked, cyclic schedule By default: Single writer per cycle, all reads initialized On demand: Separate multiple assignments by clock barrier (pause, wait) Declarative All micro-steps sequential control flow descriptive Resolved by scheduler 	 Concurrent micro-step control flow: ② Descriptive ③ Resolved by scheduler ③ ⇒ Deterministic concurrency and deadlock freedom Sequential micro-step control flow: ③ Prescriptive ③ Resolved by the programmer ③ ⇒ Intuitive programming paradigm
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 Formalizing Sequential Constructiveness (SC)
 The Control Example
 Formalizing Sequential Constructiveness (SC)
 The Control Example

 Wrap-Up
 A Constructive Game of Schedulability
 Wrap-Up
 A Constructive Game of Schedulability
 Wrap-Up
 A Constructive Game of Schedulability

Comparing Both Worlds (Cont'd)



- Asynchronous schedule
 © No guarantees of determinism
 - No guarantees of determinisr or deadlock freedom
 - Intuitive programming paradigm

Synchronous Languages

- Clocked, cyclic schedule
 - © Deterministic concurrency and deadlock freedom
 - Heavy restrictions by constructiveness analysis

Sequentially Constructive Model of Computation (SC MoC)

- $\ensuremath{\textcircled{}^\circ}$ Deterministic concurrency and deadlock freedom
- © Intuitive programming paradigm

A Sequentially Constructive Program



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A Sequentially Constructive Program (Cont'd)



A Sequentially Constructive Program (Cont'd)

Motivation

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Imperative program order (sequential access to shared variables)

- "write-after-write" can change value sequentially
- Prescribed by programmer
 - © Accepted in SC MoC

Formalizing Sequential Constructiveness (SC)

Not permitted in standard synchronous MoC ٢

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Motivation

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A Sequentially Constructive Program (Cont'd)



A Sequentially Constructive Program (Cont'd)



The Control Example

Concurrency scheduling constraints (access to shared variables):

- "write-before-read" for concurrent write/reads
- "write-before-write" (*i. e.*, conflicts!) for concurrent & non-confluent writes
- Micro-tick thread scheduling prohibits race conditions
- Implemented by the SC compiler

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A Constructive Game of Schedulability

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Organizing Concurrent Variable Accesses

Confluent Statements (per macro tick)



SC Concurrent Memory Access Protocol (per macro tick)



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concurrent, multi-writer, multi-reader variables

concurrent,

For all memorie Mem, reachable

in macro tick:

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Motivation	C, Java vs. Synchronous Programming	Motivation	C, Java vs. Synchronous Programming
Formalizing Sequential Constructiveness (SC)	The Control Example	Formalizing Sequential Constructiveness (SC)	The Control Example
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Sequential Admissibility – Basic Idea

Sequentially ordered variable accesses

- Are enforced by the programmer
- Cannot be reordered by compiler or run-time platform
- Exhibit no races
- Only concurrent writes/reads to the same variable
 - Generate potential data races
 - Must be resolved by the compiler
 - Can be ordered under multi-threading and run-time

The following applies to concurrent variable accesses only ...

Goals and Challenges

The idea behind SC is simple – but getting it "right" not so!

What we are up to:

- 1. Want to be conservative wrt "Berry constructiveness"
 - ► An Esterel program should also be SC
- 2. Want maximal freedom without compromising determinacy
 - A determinate program should also be SC
 - An SC program must be determinate
- 3. Want to exploit sequentiality as much as possible
 - But what exactly is sequentiality?
- 4. Want to define not only the exact concept of SC, but also a practical strategy to implement it
 - In practice, this requires conservative approximations
 - Compiler must not accept Non-SC programs
 - Compiler may reject SC programs

References

Motivation Formalizing Sequential Constructiveness (SC) Wrap-Up The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3] The SC Model of Computation [Sec. 4]

Most of the material here draws from this reference [TECS]:

R. von Hanxleden, M. Mendler, J. Aguado, B. Duderstadt, I. Fuhrmann, C. Motika, S. Mercer, O. O'Brien, and P. Roop.
 Sequentially Constructive Concurrency – A Conservative Extension of the Synchronous Model of Computation.
 ACM Transactions on Embedded Computing Systems, Special Issue on Applications of Concurrency to System Design, July 2014, 13(4s).
 http://rtsys.informatik.uni-kiel.de/~biblio/downloads/papers/tecs14.pdf

Unless otherwise noted, the numberings of definitions, sections etc. refer to this.

There is also an extended version [TR]:

R. von Hanxleden, M. Mendler, J. Aguado, B. Duderstadt, I. Fuhrmann, C. Motika, S. Mercer, O. O'Brien, and P. Roop.
 Sequentially Constructive Concurrency – A Conservative Extension of the Synchronous Model of Computation.
 Christian-Albrechts-Universität zu Kiel, Department of Computer Science, Technical Report 1308, ISSN 2192-6247, Aug. 2013, 13(4s).
 http://rtsys.informatik.uni-kiel.de/~biblio/downloads/papers/report-1308.pdf

The Sequentially Constructive Language (SCL) [Sec. 2.1]

Foundation for the SC MoC

Formalizing Sequential Constructiveness (SC)

- Minimal Language
- Adopted from C/Java and Esterel

 $s ::= x = e \mid s; s \mid if(e) \ s \ else \ s \mid l : s \mid goto \ l \mid fork \ s \ par \ s \ join \mid pause$



	Motivation Formalizing Sequential Constructiveness (SC) Wrap-Up	The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3] The SC Model of Computation [Sec. 4]	
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Overview

The SC Graph (SCG) [Sec. 2.3]

Motivation

Formalizing Sequential Constructiveness (SC)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3] The SC Model of Computation [Sec. 4]

Wrap-Up



The concurrent and sequential control flow of an SCL program is given by an SC Graph (SCG)

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]

Internal representation for

Semantic foundation

Free Scheduling of SCGs [Sec. 3] The SC Model of Computation [S

- Analysis
- Code generation

SC Graph:

Labeled graph G = (N, E)

- Nodes N correspond to statements of sequential program
- Edges E reflect sequential execution control flow

Motivation The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Formalizing Sequential Constructiveness (SC) Free Scheduling of SCGs [Sec. 3] Wrap-Up The SC Model of Computation [Sec. 4]	Motivation The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Formalizing Sequential Constructiveness (SC) Free Scheduling of SCGs [Sec. 3] Wrap-Up The SC Model of Computation [Sec. 4]		
Node Types in the SCG	Edge Types in the SCG [Def. 2.1]		
	Edge $e \in E$ has edge type $e.type \in \alpha_a$		
	 Specifies the nature of the particular ordering constraint expressed by e 		
Node $n \in N$ has statement type <i>n.st</i>	► For $e.type = \alpha$, write $e.src \rightarrow_{\alpha} e.tgt$, pronounced "e.src α -precedes $e.tgt$ "		
{entry, exit, goto, $x = ex$, if (ex) , fork, join, surf, depth}	▶ $n_1 \rightarrow_{seq} n_2$: sequential successors		
 x: variable, ex: expression. 	► $n_1 \rightarrow_{tick} n_2$: tick successors		
	▶ $n_1 \rightarrow_{seq} n_2$, $n_1 \rightarrow_{tick} n_2$: flow successors, induced directly from source program		
	▶ \rightarrow seq: reflexive and transitive closure of \rightarrow seq		
	▶ Note: $n_1 \rightarrow_{seq} n_2$ does not imply fixed run-time ordering between n_1 and n_2 (consider loops)		
C A U Synchronous Languages Lecture 13 Slide 21	C A U Synchronous Languages Lecture 13 Slide 23		
Motivation The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Formalizing Sequential Constructiveness (SC) Free Scheduling of SCGs [Sec. 3] Wrap-Up The SC Model of Computation [Sec. 4]	Motivation The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Formalizing Sequential Constructiveness (SC) Free Scheduling of SCGs [Sec. 3] Wrap-Up The SC Model of Computation [Sec. 4]		
Edge Types in the SCG [Def. 2.1]	Mapping SCL & SCG		
	ThreadConcurrencyConditionalAssignmentDelay(Region)(Superstate)(Trigger)(Effect)(State)		
Define edge types:			
• iur-edges $\alpha_{iur} =_{def} \{ww, iu, ur, ir\}$	SCG		

- instantaneous edges $\alpha_{ins} =_{def} \{seq\} \cup \alpha_{iur}$
- arbitrary edges $\alpha_a =_{def} \{tick\} \cup \alpha_{ins}$
- flow edges $\alpha_{flow} =_{def} \{seq, tick\}$

fork t_1 par t_2 join if $(c) s_1$ else s_2

join

exit

t

SCL

depth

pause

x = e

SCL & SCG – The Control Example



Motivation The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Formalizing Sequential Constructiveness (SC) Wran-Iba The SC Model of Computation [Sec. 4]

Sequentiality vs. Concurrency Static vs. Dynamic Threads

Recall: We want to distinguish between *sequential* and *concurrent* control flow.

But what do "sequential" / "concurrent" mean?

This distinction is not as easy to formalize as it may seem

To get started, distinguish

- Static threads: Structure of a program (based on SCG)
- Dynamic thread instance: thread in execution

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Static Threads [Sec. 2.4]

- Given: SCG G = (N, E)
- Let T denote the set of threads of G
- ► *T* includes a top-level Root thread
- With each thread $t \in T$, associate unique
 - entry node $t_{en} \in N$
 - exit node $t_{ex} \in N$
- Each $n \in N$ belongs to a thread th(n) defined as
 - Immediately enclosing thread $t \in T$
 - such that there is a flow path to n that originates in t_{en}, does not traverse t_{ex},¹ and does not traverse any other entry node t'_{en}, unless that flow path subsequently traverses t'_{ex} also

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For each thread t, define sts(t) as the

set of statement nodes $n \in N$ such that th(n) = t

¹Added to definition in paper! c|A|U Synchronous Languages

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Threads in Control Example



- ► Threads *T* = {*Root*, *Request*, *Dispatch*}
- Root thread consists of the statement nodes sts(Root) = {L0, L7, L28, L29}
- The remaining statement nodes of N are partitioned into sts(Dispatch) and sts(Request)

Static Thread Concurrency and Subordination [Def. 2.2]

Let t_1 , t_1 , t_2 be threads in T

- fork(t) = def fork node immediately preceding t_{en}
- For every thread $t \neq \text{Root}$: $p(t) =_{def} th(fork(t))$, the parent thread
- $p^*(t) =_{def} \{t, p(t), p(p(t)), \dots, \text{Root}\}$, the recursively defined set of ancestor threads of t
- t_1 is subordinate to t_2 , written $t_1 \prec t_2$, if $t_1 \neq t_2 \land t_1 \in p^*(t_2)$
- ▶ t_1 and t_2 are (statically) concurrent, denoted $t_1 \parallel t_2$, iff t_1 and t_2 are descendants of distinct threads sharing a common fork node. *i.e.*:
 - $\exists t'_1 \in p^*(t_1), t'_2 \in p^*(t_2) : t'_1 \neq t'_2 \land fork(t'_1) = fork(t'_2)$
 - Denote this common fork node as $lcafork(t_1, t_2)$, the least common ancestor fork
 - Lift (static) concurrency notion to nodes: $n_1 \parallel n_2 \Leftrightarrow$ $th(n_1) || th(n_2) \Leftrightarrow lcafork(n_1, n_2) = lcafork(th(n_1), th(n_2))$

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The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]

Free Scheduling of SCGs [Sec. 3]

Thread Trees [TR, Sec. 3.7]

A Thread Tree illustrates the static thread relationships.

- Contains subset of SCG nodes:
 - 1. Entry nodes, labeled with names of their threads
 - 2. Fork nodes, attached to the entry nodes of their threads
- Similar to the AND/OR tree of Statecharts

Thread tree for Control example:

Formalizing Sequential Constructiveness (SC)





- \blacktriangleright Root \prec Request and Root \prec Dispatch
- ▶ *Request* || *Dispatch*, *Root* is not concurrent with any thread

Note: Concurrency on threads, in contrast to concurrency on node instances, is purely static and can be checked with a simple, syntactic analysis of the program structure.



Concurrency and Subordination in Control-Program

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Thread Reincarnation – The Reinc Example





Not enough to impose an order on the program statements \Rightarrow Need to distinguish statement instances

Statement Reincarnation II



- Traditional synchronous languages: Reject
- Instantaneous loops traditionally forbidden
- One might still want to ensure that a program always terminates
- But this issue is orthogonal to determinacy and having a well-defined semantics.

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Macroticks [Def. 2.3 + 2.4]

- Given: SCG G = (N, E)
- (Macro) tick R, of length len(R) ∈ N≥1: mapping from micro tick indices 1 ≤ j ≤ len(R), to nodes R(j) ∈ N

A macro tick is also: Linearly ordered set of node instances

- Node instance: ni = (n, i), with statement node n ∈ N, micro tick count i ∈ N
- Can identify macro tick R with set $\{(n,i) \mid 1 \le i \le len(R), n = R(i)\}$

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Free Scheduling of SCGs [Sec. 3]	
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Run-Time Concurrency [Def. 2.5 + 2.6]

Given: macro tick R, index $1 \le i \le len(R)$, node $n \in N$ Def.: $last(n, i) = max\{j \mid j \le i, R(j) = n\}$, retrieves last occurrence of n in R at or before index i. If it does not exist, $last_R(n, i) = 0$.

Given: macro tick R, $i_1, i_2 \in \mathbb{N}_{\leq len(R)}$, and $n_1, n_2 \in N$. Def.: Two node instances $ni_1 = (n_1, i_1)$ and $ni_2 = (n_2, i_2)$ are (run-time) concurrent in R, denoted $ni_1 \mid_R ni_2$, iff

- 1. they appear in the micro ticks of R, *i.e.*, $n_1 = R(i_1)$ and $n_2 = R(i_2)$,
- 2. they belong to statically concurrent threads, *i. e.*, $th(n_1) \parallel th(n_2)$, and
- their threads have been instantiated by the same instance of the associated least common ancestor fork, *i. e.*, *last*(n, i₁) = *last*(n, i₂) where n = *lcafork*(n₁, n₂)
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Continuations & Thread Execution States [Def. 3.1]

A continuation *c* consists of

- Node *c.node* ∈ *N*, denoting the current state of each thread, *i. e.*, the node (statement) that should be executed next, similar to a program counter
- 2. Status $c.status \in \{active, waiting, pausing\}$



In a trace (see later slide), round/square/no parentheses around n = c.node denote *c.status*, for enabled continuations *c*



Motivation

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Wrap-Up

Continuation pool: finite set C of continuations

 C is valid if C meets some coherence properties (see [TECS]), e. g., threads in C adhere to thread tree structure

Configuration: pair (C, M)

- ► C is continuation pool
- M is memory assigning values to variables accessed by G

A configuration is called valid if C is valid



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Now define free scheduling, to set the stage for later defining

• If there is at least one continuation in C_{cur} , then there also is a \prec -maximal one, because of the finiteness of the continuation

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Micro step: transition $(C_{cur}, M_{cur}) \xrightarrow{c} (C_{nxt}, M_{nxt})$ between two

The free schedule is permitted to pick any one of the \prec -maximal continuations $c \in C_{cur}$ with c.status = active and execute it in the Formalizing Sequential Constructiveness (SC)

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The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3] The SC Model of Computation

Micro Steps II

(Recall:) Micro step: transition $(C_{cur}, M_{cur}) \xrightarrow{c} U_{us} (C_{nxt}, M_{nxt})$

- Executing c yields a new memory $M_{nxt} = \mu M(c, M_{cur})$ and a (possibly empty) set of new continuations $\mu C(c, M_{cur})$ by which *c* is replaced, *i.e.*, $C_{nxt} = C_{cur} \setminus \{c\} \cup \mu C(c, M_{cur})$
- If $\mu C(c, M_{cur}) = \emptyset$: status flags set to active for all $c' \in C_{nxt}$ that become \prec -maximal by eliminating c from C
- Actions μM and μC (made precise in paper) depend on the statement *c.node.st* to be executed
- $(C_{n\times t}, M_{n\times t})$ uniquely determined by c, thus may write $(C_{n\times t}, M_{n\times t}) = c(C_{cur}, M_{cur})$

Clock Steps II

Global clock step V_I : $(C_{cur}, M_{cur}) \rightarrow_{tick} (C_{nxt}, M_{nxt})$

- Transition between last micro tick of the current macro tick to first micro tick of the subsequent macro tick
- \blacktriangleright V₁ is external input
- \blacktriangleright All pausing continuations of C advance from their surf node to the associated depth node:

$$C_{nxt} = \{c[active :: tick(n)] \mid c[pausing :: n] \in C_{cur}\} \cup \\ \{c[waiting :: n] \mid c[waiting :: n] \in C_{cur}\}$$



- No active $c \in C$
- ▶ All $c \in C$ pausing or waiting

If $C = \emptyset$:

Main program terminated

Otherwise:

Scheduler can perform a global clock step

- Let $I = \{x_1, x_2, \dots, x_n\}$ be the designated input variables of the SCG, including input/output variables
- Memory is updated by a new set of external input values $V_l = [x_1 = v_1, \dots, x_n = v_n]$ for the next macro tick
- All other memory locations persist unchanged into the next macro tick.

Formally,

$$M_{nxt}(x) = \begin{cases} v_i, & \text{if } x = x_i \in I, \\ M_{cur}(x), & \text{if } x \notin I. \end{cases}$$

Macro Ticks

Scheduler runs through sequence

$$(C_0^a, M_0^a) \stackrel{c_1^a}{\to}_{\mu s} (C_1^a, M_1^a) \stackrel{c_2^a}{\to}_{\mu s} \cdots \stackrel{c_{k(a)}^a}{\to}_{\mu s} (C_{k(a)}^a, M_{k(a)}^a)$$
(1)

to reach final quiescent configuration $(C^a_{k(a)}, M^a_{k(a)})$

Sequence (1) is macro tick (synchronous instant) *a*:

$$(R^a, V_I^a) : (C_0^a, M_0^a) \Longrightarrow (C_{k(a)}^a, M_{k(a)}^a)$$

$$\tag{2}$$

- V_I^a : projects the initial input, $V_I^a(x) = M_0^a(x)$ for $x \in I$
- $M_{k(a)}^{a}$: response of a

 R^a : sequence of statement nodes executed during a

- $len(R^a) = k(a)$ is length of a
- *R^a* is function mapping each micro tick index 1 ≤ j ≤ k(a) to node *R^a(j) = c_i^a.node* executed at index j

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Determinacy

Recall:

- ► Macro (tick) configuration: end points of a macro tick (2)
- ► Micro (tick) configuration: all other intermediate configurations (C^a_i, M^a_i), 0 < i < k(a) seen in (1)</p>

Synchrony hypothesis:

- only macro configurations are observable externally (in fact, only the memory component of those)
- ► Suffices to ensure that sequence of macro ticks ⇒ is determinate
- Micro tick behavior $\rightarrow_{\mu s}$ may well be non-determinate

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Formalizing Sequential Constructiveness (SC)

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 The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]

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 Wrap-Up
 The SC Model of Computation [Sec. 4]

Runs and Traces

Run of G: sequence of macro ticks R^a and external inputs V_I^a , with

- ▶ initial continuation pool C₀⁰ = {c₀} activates the entry node of the G's Root thread, i.e., c₀.node = Root.en and c₀.status = active
- ▶ all macro tick configurations are connected by clock steps, i.e., $(C^a_{k(a)}, M^a_{k(a)}) \rightarrow_{tick} (C^{a+1}_0, M^{a+1}_0)$

Trace: externally visible output values at each macro tick R [TR, Sec. 3.9]

Active and Pausing Continuations are Concurrent [TR, Prop. 2]

Given:

- (C, M), reachable (micro or macro tick) configuration
- ▶ $c_1, c_2 \in C$, active or pausing continuations with $c_1 \neq c_2$

Then:

- $c_1.node \neq c_2.node$
- $th(c_1.node) \parallel th(c_2.node)$

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► No instantaneous sequential path from c₁.node to c₂.node or vice versa

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(Proof: see [TR])

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The SC Language (SCL) and the SC Graph (SCG) [Sec. Free Scheduling of SCGs [Sec. 3]

Concurrency vs. Sequentiality Revisited I

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3] The SC Model of Computation [Sec. 4]

Notes on Free Scheduling I

Recall: Want to exploit sequentiality as much as possible

• Thus, consider only run-time concurrent data dependencies

Recall: Static concurrency \neq run-time concurrency

- Consider Reinc example
- > Thus, can ignore some statically concurrent data dependencies

Key to determinacy:

rule out uncertainties due to unknown scheduling mechanism

- Like the synchronous MoC, the SC MoC ensures macro-tick determinacy by inducing certain scheduling constraints on variable accesses
- Unlike the synchronous MoC, the SC MoC tries to take maximal advantage of the execution order already expressed by the programmer through sequential commands
- A scheduler can only affect the order of variable accesses through concurrent threads

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Question: Does (st time concurrency?	tatic) sequenti	ality preclude run-	entry	Recall:	o accesses (within ti	ck) are alread	du coquentialized bu
 Then we could between nodes But the approximation 	d ignore data o s that are sequ	dependencies ientially ordered		\rightarrow_{seq} , th continua	e accesses (within the ey cannot appear sir tion pool	nultaneously	in the active
Counterexample: F	Reinc3 (SCG sl	nown on right)	x=1 x=2	 Hence, n lead to a Similarly, three 	o way for thread sch non-determinate ou pade are not concurre	eduler to rec itcome	order them and thus
Assignments tAssignments t	to x run-time o to x sequential	oncurrent? Yes! ly ordered? Yes!		 Because suspende 	of path ordering \prec , d when a child threa	a parent thread is in opera	ead is always ation
Thus, concurrency not mutually excl	<pre>/ and (static) usive, but or</pre>	sequentiality are hogonal!		 Thus, no thread 	t up to scheduler to	decide betw	een parent and child
However, (Instant (on node <i>instances</i> rency	aneous) run-t 5) does exclude	run-time concur-	exit	 No race parent ar 	conditions between v nd child threads; no	variable acces source of no	sses performed by n-determinacy

Motivation Formalizing Sequential Constructiveness (SC) The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3] The SC Model of Computation [Sec. 4]

The Aim

Want to find a suitable restriction on the "free" scheduler which is

- 1. easy to compute
- 2. leaves sufficient room for concurrent implementations
- still (predictably) sequentializes any concurrent variable accesses that may conflict and produce unpredictable responses

In the following, will define such a restriction: the SC-admissible schedules

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Guideline for SC-admissibility

- Initialize-Update-Read protocol, for concurrent accesses
- Want to conservatively extend Esterel's "Write-Read protocol" (must do emit *before* testing)
- ▶ But does Esterel *always* follow write-read protocol?

Write After Read Revisited

module WriteAfterRead		entry
output x, y, z;	markel a Musit al ft an Daad	¥ x = 1
	module writeArterRead	
emit x;	output int x, y, z;	fork
[{	
present x then	x = 1;	entry
emit y	fork	entry
end	y = x;	
11	par	z = y
present y then	z = y;	y=x
emit z	x = 1;	×-1
end;	join	exit
emit x	}	exit
]	L	
end	SCL version	join
F		exit
F		exit

Esterel version

- Concurrent emit after present test
- But WriteAfterRead is BC hence should also be SC!
- Observation: second emit is ineffective, *i. e.*, does not change value
- One approach: permit concurrent ineffective writes after read

Ineffectiveness - 1st Try [TR, Sec. 5.2]

1	module InEffective1	
2	output int $x = 2$:	
3	int v;	
4	{	
5	fork	
6	if (x == 2) {	
7	y = 1;	
8	x = 7	
9	}	
10	else	
11	y = 0	
12	par	
13	x = 7	
14	join	
15	}	

- If L13 is scheduled before L6:
 - ► L13 is effective
- No out-of-order write
- ► y = 0

If L13 is scheduled after L8 (and L6):

- ► L13 is out-of-order write
- ► However, L13 is ineffective
- $y = 1 (\rightarrow non-determinacy!)$
- The problem: L8 hides the potential effectiveness of L13 wrt. L6!
- Both schedules would be permitted under a scheduling regime that permits ineffective writes
- \blacktriangleright \rightarrow Strengthen notion of "ineffective writes":
- Consider writes "ineffective" only if they do not change read!

Ineffectiveness – 2nd Try

		x = x xor true
1	module InEffective2	Relative w
2	output bool x = false;	
3	int y;	Equivalent
4	{	Sequence 13
5	fork	Sequence L10,
6	if (!x) {	► y = 0
7	y = 1;	
8	x = x xor true	Sequence Lb; L
9	}	▶ <u>0</u> · ls 13
10	else	Q. 15 E15
11	y = 0	A: Yes!
12	par	. 112
13	x = x xor true;	LI3 IS OUT
14	join	but writes
15	}	l 6 roodi
		i n readi

- e" /rites to "x = !x" L6; L11: _7; L8; L13: ineffective relative to L6? -of-order . . .
- x = true, which is what Lb read!
- ▶ y = 1 (→ again non-determinacy!)
- Again, both schedules would be permitted under a scheduling regime that permits ineffective writes
- \blacktriangleright \rightarrow Replace "ineffectiveness" by "confluence"

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3] The SC Model of Computation [Sec. 4]

Combination Functions [Def. 4.1]

Combination function f:

- $f(f(x, e_1), e_2) = f(f(x, e_2), e_1)$ for all x and all side-effect free expressions e_1, e_2
- ► Sufficient condition: *f* is *commutative* and *associative*
- ► Examples: *, +, -, max, and, or

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Motivation The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Formalizing Sequential Constructiveness (SC) Free Scheduling of SCGs [Sec. 3] Wrap-Up The SC Model of Computation [Sec. 4]	Motivation The SC Language (SCL) and the SC Graph (SCG) [Sec. Formalizing Sequential Constructiveness (SC) Free Scheduling of SCGs [Sec. 3] Wrap-Up The SC Model of Computation [Sec. 4]			
Dverview	Relative and Absolute Writes [Def. 4.2]			
	Relative writes, of type f ("increment" / "modify"): $x = f(x, e)$			
Motivation	f must be a combination function			
	Evaluation of e must be free of side effects			
Formalizing Sequential Constructiveness (SC)	Thus, schedules			
The SC Language (SCL) and the SC Graph (SCG) [Sec. 2]	$x = f(x, e_1); x = f(x, e_2)'$ and			
Free Scheduling of SCGs [Sec. 3]	'x = f(x, e ₂); x = f(x, e ₁)' yield same result for x ► Thus, writes are confluent			
The SC Model of Computation [Sec. 4]				
	► E.g., x++, x = 5 * x, x = x-10			
Wrap-Up	Absolute writes ("write" / "initialize"): $x = e$			
	 Writes that are not relative 			
	► E.g., $x = 0$, $x = 2*y+5$, $x = f(z)$			
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Formalizing Sequential Constructiveness (SC)

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iur Relations [Def. 4.3]

Given two statically concurrent accesses $n_1 \parallel n_2$ on some variable x, we define the jur relations

- ▶ $n_1 \rightarrow_{ww} n_2$ iff n_1 and n_2 both initialize x or both perform updates of different type. We call this a ww conflict
- ▶ $n_1 \rightarrow_{in} n_2$ iff n_1 initializes x and n_2 updates x
- ▶ $n_1 \rightarrow_{ur} n_2$ iff n_1 updates x and n_2 reads x
- ▶ $n_1 \rightarrow_{ir} n_2$ iff n_1 initializes x and n_2 reads x

Synchronous Languages

Since $n_1 \rightarrow_{ww} n_2$ implies $n_2 \rightarrow_{ww} n_1$:

- ▶ abbreviate the conjunction of $n_1 \rightarrow_{ww} n_2$ and $n_2 \rightarrow_{ww} n_1$ with $n_1 \leftrightarrow_{ww} n_2$
- \blacktriangleright by symmetry \rightarrow_{ww} implies \leftrightarrow_{ww}

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2

Free Scheduling of SCGs [Sec. 3]

Notes on Confluence

(From definition:) $n_1 \sim_{(C,M)} n_2$ iff

▶ \exists Sequence of micro steps $(C, M) \rightarrow_{us} (C', M')$ such that n_1 and n_2 are conflicting in (C', M')

Observations I

- Confluence is taken relative to valid configurations (C, M) and *indirectly* as the absence of conflicts
- Instead of requiring that confluent nodes commute with each other for arbitrary memories, we only consider those configurations (C', M') that are *reachable* from (C, M)
- E.g., if it happens for a given program that in all memories M' reachable from a configuration (C, M) two expressions ex_1 and e_{x_2} evaluate to the same value, then the assignments x = ex_1 and $x = ex_2$ are confluent in (C, M)
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Motivation Formalizing Sequential Constructiveness (SC)	The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3]
Wrap-Up	The SC Model of Computation [Sec. 4]

Lecture 13

Confluence of Nodes [Def. 4.4]

Given:

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- \blacktriangleright Valid configuration (C, M) of SCG
- ▶ Nodes $n_1, n_2 \in N$

```
n_1, n_2 are conflicting in (C, M) iff
```

- 1. n_1, n_2 active in C,
 - *i. e.*, $\exists c_1, c_2 \in C$ with $c_i.status = active and n_i = c_i.node$
- 2. $c_1(c_2(C, M)) \neq c_2(c_1(C, M))$

 n_1, n_2 are confluent with each other in (C, M), written: $n_1 \sim (C,M) n_2$, iff

► \exists Sequence of micro steps $(C, M) \rightarrow_{\mu s} (C', M')$ such that n_1 and n_2 are conflicting in (C', M')

Formalizing Sequential Constructiveness (SC) The SC Model of Computation [Sec. 4] Notes on Confluence

- (From definition:) $n_1 \sim_{(C,M)} n_2$ iff
 - ▶ \exists Sequence of micro steps $(C, M) \rightarrow_{us} (C', M')$ such that n_1 and n_2 are conflicting in (C', M')

Observations II

- Similarly, if the two assignments are never jointly active in any reachable continuation pool C', they are confluent in (C, M), too
- Thus, statements may be confluent for some program relative to some reachable configuration, but not for other configurations or in another program
- ▶ However, notice that relative writes of the same type are confluent in the absolute sense, *i. e.*, for all valid configurations (C, M) of all programs

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Notes on Confluence

(From definition:) $n_1 \sim_{(C,M)} n_2$ iff

► \exists Sequence of micro steps $(C, M) \rightarrow_{\mu s} (C', M')$ such that n_1 and n_2 are conflicting in (C', M')

Observations III

- ▶ Confluence $n_1 \sim_{(C,M)} n_2$ requires conflict-freeness for all configurations (C', M') reachable from (C, M) by arbitrary micro-sequences under free scheduling
- Will use this notion of confluence to define the restricted set of SC-admissible macro ticks
- Since compiler will ensure SC-admissibility of the execution schedule.

one might be tempted to define confluence relative to these SC-admissible schedules;

however, this would result in a logical cycle

CAU Synchronous Languages Lecture 13

The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3] Formalizing Sequential Constructiveness (SC) The SC Model of Computation [Sec. 4]

Notes on Confluence

(From definition:) $n_1 \sim_{(C,M)} n_2$ iff

► \exists Sequence of micro steps $(C, M) \rightarrow_{us} (C', M')$ such that n_1 and n_2 are conflicting in (C', M')

Observations IV

- This relative view of confluence keeps the scheduling constraints on SC-admissible macro ticks sufficiently weak
- Note: two nodes confluent in some configuration are still confluent in every later configuration reached through an arbitrary sequence of micro steps
- However, more nodes may become confluent in later configurations, because some conflicting configurations are no longer reachable
- Exploit this in following definition of confluence *of node* instances by making confluence of node instances within a macro tick relative to the index position at which they occur

The SC Language (SCL) and the SC Graph (SCG) [Sec. Free Scheduling of SCGs [Sec. 3] The SC Model of Computation [Sec. 4]

Confluence of Node Instances [Def. 4.5]

Given:

- Macro tick R
- (C_i, M_i) for 0 < i < len(R), the configurations of R
- ▶ Node instances $ni_1 = (n_1, i_1)$ and $ni_2 = (n_2, i_2)$ in R, *i. e.*, $1 \leq i_1, i_2 \leq len(R), n_1 = R(i_1), n_2 = R(i_2)$

Lecture 13

Call node instances confluent in R, written $ni_1 \sim_R ni_2$, iff

- for $i = min(i_1, i_2) 1$
- \triangleright $n_1 \sim_{(C_i,M_i)} n_2$

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InEffective2 Revisited

1 2	<pre>module InEffective2 output bool x = false;</pre>	Recall sequence L6; L7; L8; L13:
3	int y;	Q: Is L13 ineffective relative to L6?
4	{	
5	tork	A. 103:
6	if (!x) {	113 is out-of-order
7	v = 1;	
8	x = x xor true	but writes x = false, which is what
9	}	1.6 road
10	else	LU reau!
11	у = 0	Q: Are L6 and L13 confluent?
12	par	
13	x = x xor true;	► A: No!
14	join	I 6 and I 13 conflict at point of
15	}	execution of 1.6

 \rightarrow Def. of SC-admissibility – specifically, the underlying scheduling relations - uses confluence condition

Motivation Formalizing Sequential Constructiveness (SC) The SC Language (SCL) and the SC Graph (SCG) [Sec. 2] Free Scheduling of SCGs [Sec. 3] The SC Model of Computation [Sec. 4]

Scheduling Relations [Def 4.6]

SC-admissibility vs. Determinacy





Example $P_{APS} = if(x) x = 1$

Acyclic Schedulable

(ASC)

Acyclic Schedulable (ASC)

or concurrent writes

NonDet

All Programs

Cycle of concurrent pendencies

Out-of-order

scheduling

Logically Correct (LC)

 P_L

Synchronous Program Classes





Synchronous Program Classes



Example $P_{ALPS} = if (!x \&\& y) \{x = 1; y = 1\}$

Synchronous Program Classes



Motivation Synchronous Program Classes Formalizing Sequential Constructiveness (SC) Summary

Summary

Underlying idea of sequential constructiveness rather simple

- Prescriptive instead of descriptive sequentiality
- Thus circumventing "spurious" causality problems
- Initialize-update-read protocol

However, precise definition of SC MoC not trivial

- Challenging to ensure conservativeness relative to Berry-constructiveness
- Plain initialize-update-read protocol does not accomodate, e. g., signal re-emissions
- Restricting attention to *concurrent*, *non-confluent* node instances is key

Example $P_{ALS} = \text{if } (!x) x = 1 \text{ else } x = 1$

shared-memory multi-threading

standard sequential control flow (Java, C)

► ☺ Predictable concurrent threads

 Deterministic concurrency with synchronous foundations, but without synchronous restrictions

• ③ Expressive and intuitive sequential paradigm

Synchronous Program Classes Summary

Clocked, synchronous model of execution for imperative,

Conservatively extends synchronous programming (Esterel) by

Synchronous Program Classes Summary

Future Work

Plenty of extensions/adaptations possible

- Alternative notions of sequential constructiveness:
 - A truly "constructive" approach that sharpens SC admissibility to determinate schedules
 - ► Extension of iur-protocol, *e.g.*, to model ForeC
- ► Improved synthesis & analysis see also next lecture

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